

Master of Science

Mathematics

AY: 2018- 19

Program and Course Structure

**School of Basic Science and Research
Department of Mathematics**

M. Sc. (Mathematics)

SBR0301

Batch 2018-20

1.1 Vision, Mission and Core Values of the University

Vision of the University

To serve the society by being a global University of higher learning in pursuit of academic excellence, innovation and nurturing entrepreneurship.

Mission of the University

1. Transformative educational experience.
2. Enrichment by educational initiatives that encourage global outlook.
3. Develop research, support disruptive innovations and accelerate Entrepreneurship.
4. Seeking beyond boundaries.

Core Values

1. Integrity
2. Leadership
3. Diversity
4. Community

1.2 Vision and Mission of the School

Vision of the School

Achieving excellence in the realm of science to address the challenges of evolving society

Mission of the School

1. Equip the students with knowledge and skills
2. Capacity building by providing academic flexibility to student and faculty members
3. To establish centre of excellence for innovative research
4. Address the deficiencies of the society pertaining to environment
5. To strengthen academic- industry collaboration for better employability
6. Developing a culture for continued betterment in all facets of life

Core Values

1. Integrity
2. Leadership
3. Diversity
4. Community

1.3 Vision and Mission

Department of Mathematics

Vision of the Department

To become a globally recognized destination for education in applied mathematics and research.

Mission of the Department

1. To develop mathematical skills in students and make them employable across a wide range of professions and promote interest research.
2. To develop entrepreneurial skills in students to serve the society at large.
3. To develop skills for the applications of mathematics in the various fields.

Core Values

1. Integrity
2. Leadership
3. Diversity
4. Community

M. Sc. (Mathematics)

1.4 Programme Educational Objectives (PEO's)

PEO1: To deliver deep subject knowledge in the courses of study to enable students to shine in various fields such as sciences, engineering and technology, IT etc.

PEO2: To develop positive attitude and skills to enable the students to become a multi facet personality.

PEO3: To prepare students for entrance examinations conducted by IIT's/Universities to pursue Ph. D. programs as well as NET, UGC-CSIR.

PEO4: To develop students to be excellent to be excellent communicators and team players.

1.4.1 Program Outcomes (PO's)

PO1:Mathematical knowledge:Application of Mathematical knowledge in various fields of science, engineering and management etc.

PO2:Nature of Mathematics:Understand the concise, precise and rigorous nature of Mathematics.

PO3: Critical thinking:Develop the skill to think critically on abstract concepts of Mathematics.

PO4:Problem analysis: Develop the ability to analyze a problem logically and dissect into micro-parts and thus resolving the problem to accessible components.

PO5: Mathematical logic and Ethics:Formulates and develops mathematical arguments in logical manner and Realize and understand professional, ethical and cultural responsibilities.

1.4.2 Programme Specific Outcomes (PSO's)

PSO1 : Scientific thinking and logical abilities.

PSO2 : Application of Mathematical principles in practical situations and software developments.

PSO3 : Analyze any problem to micro-levels and solve the problem step by step.

PSO4 : Owning up responsibility for logical comprehension and preparedness for constant improvement.

1.4.2 Map PEOs with Mission Statements:

| PEO Statements | School Mission 1 | School Mission 2 | School Mission 3 | School Mission 4 | School Mission 5 | School Mission 6 |
|-----------------------|-------------------------|-------------------------|-------------------------|-------------------------|-------------------------|-------------------------|
| PEO1: | 3 | 2 | 3 | 1 | 2 | 3 |
| PEO2: | 3 | 2 | 3 | 1 | 2 | 3 |
| PEO3: | 3 | 3 | 3 | 3 | 3 | 3 |
| PEO4: | 3 | 2 | 3 | 1 | 3 | 3 |

1.4.3 Mapping of Program Outcome (PO's) Vs Program Educational Objectives (PEO's)

| | PEO1 | PEO2 | PEO3 | PEO4 |
|-------------|-------------|-------------|-------------|-------------|
| PO1 | 3 | 3 | 3 | 2 |
| PO2 | 3 | 3 | 3 | 2 |
| PO3 | 3 | 3 | 3 | 2 |
| PO4 | 3 | 2 | 3 | 2 |
| PO5 | 2 | 3 | 2 | 3 |
| PSO1 | 2 | 2 | 3 | 2 |
| PSO2 | 3 | 2 | 2 | 3 |
| PSO3 | 3 | 3 | 2 | 3 |
| PSO4 | 3 | 2 | 3 | 3 |

1. Slight (Low)

2. Moderate (Medium)

3. Substantial (High)

1.3.5 Program Outcome (PO's)Vs Courses Mapping Table:

1.3.5.1 COURSE ARTICULATION MATRIX

| Co's | PO1 | PO2 | PO3 | PO4 | PO5 | PSO1 | PSO2 | PSO3 | PSO4 |
|---------|-----|-----|-----|-----|-----|------|------|------|------|
| MMT-101 | 3 | 2 | 2 | 3 | 2 | 3 | 3 | 2 | 2 |
| MMT-102 | 3 | 2 | 2 | 3 | 3 | 3 | 2 | 2 | 2 |
| MMT-104 | 3 | 2 | 2 | 3 | 2 | 3 | 3 | 2 | 2 |
| MMT-105 | 3 | 2 | 2 | 3 | 2 | 3 | 3 | 2 | 2 |
| MMT-119 | 3 | 2 | 2 | 3 | 2 | 3 | 3 | 2 | 2 |
| MMT-151 | 3 | 3 | 2 | 3 | 3 | 3 | 3 | 3 | 3 |
| MMT-113 | 3 | 2 | 2 | 3 | 2 | 3 | 3 | 2 | 2 |
| MMT-106 | 3 | 2 | 3 | 3 | 2 | 3 | 3 | 2 | 2 |
| MMT-107 | 3 | 2 | 2 | 3 | 2 | 3 | 3 | 2 | 2 |
| MMT-108 | 3 | 2 | 3 | 3 | 3 | 3 | 3 | 2 | 2 |
| MMT-152 | 3 | 3 | 2 | 2 | 3 | 3 | 3 | 3 | 3 |
| MMT-201 | 3 | 2 | 2 | 3 | 3 | 3 | 2 | 2 | 2 |

| | | | | | | | | | |
|---------|---|---|---|---|---|---|---|---|---|
| MMT-203 | 3 | 2 | 2 | 3 | 2 | 3 | 3 | 2 | 2 |
| MMT-209 | 3 | 3 | 3 | 3 | 2 | 3 | 2 | 2 | 2 |
| MMT-204 | 3 | 2 | 2 | 3 | 3 | 3 | 3 | 2 | 2 |
| MMT-206 | 3 | 2 | 2 | 3 | 2 | 3 | 2 | 2 | 2 |
| MMT-251 | 3 | 3 | 2 | 2 | 3 | 3 | 3 | 2 | 3 |
| MMT-252 | 2 | 3 | 2 | 2 | 3 | 3 | 3 | 3 | 2 |
| MMT-205 | 3 | 2 | 2 | 3 | 3 | 3 | 3 | 2 | 2 |
| MMT-202 | 3 | 2 | 2 | 3 | 2 | 3 | 2 | 2 | 2 |
| MMT-208 | 3 | 3 | 2 | 3 | 2 | 3 | 3 | 2 | 2 |
| MMT-253 | 2 | 3 | 2 | 2 | 3 | 3 | 3 | 3 | 3 |

1-Slight (Low)

2-Moderate (Medium)

3-Substantial (High)

Department of Mathematics
School of Basic Sciences & Research
M. Sc. (Mathematics)
Batch: 2018-20

TERM: I

| S. No. | SUBJECT CODE | Title of Paper | HOURS | | | | CREDITS | PRE-REQUISITE/ CO-REQUISITE | Type of Course ¹ : 1. CC 2. AECC 3. SEC 4. DSE |
|--------------|-------------------|--|-----------|----------|----------|--------------|---------|--------------------------------|---|
| | THEORY | | L | T | P | TOTAL | | | |
| 1. | MMT 101 | REAL ANALYSIS | 4 | - | - | 4 | 4 | CO-REQUISITE | CC |
| 2. | MMT 102 | LINEAR ALGEBRA | 4 | - | - | 4 | 4 | CO-REQUISITE | CC |
| 3. | MMT 105 | ORDINARY & PARTIAL DIFFERENTIAL EQUATIONS | 4 | - | - | 4 | 4 | CO-REQUISITE | CC |
| 4. | MMT 104 | STATISTICAL METHODS | 4 | - | - | 4 | 4 | CO-REQUISITE | CC |
| 5. | MMT 119 | INTRODUCTION to MATLAB AND ITS APPLICATIONS | 3 | - | - | 3 | 2 | CO-REQUISITE | AECC |
| | PRACTICALS | | | | | | | | |
| 6. | MMT 151 | MATHEMATICS LAB- I | - | - | 3 | 3 | 2 | CO-REQUISITE | AECC |
| TOTAL | | | 19 | - | 3 | 22 | | | 20 |

¹ CC: Core Course, AECC: Ability Enhancement Compulsory Courses, SEC: Skill Enhancement Courses, DSE: Discipline Specific Courses

Department of Mathematics
School of Basic Sciences & Research
M. Sc. (Mathematics)
Batch: 2018-2020
TERM: II

| S. No. | SUBJECT CODE | Title of Paper | HOURS | | | | CREDITS | PRE-REQUISITE/ CO-REQUISITE | Type of Course ² : |
|--------------|-------------------|---|-----------|----------|----------|-----------|-----------|--------------------------------|-----------------------------------|
| | | | L | T | P | TOTAL | | | 5. CC 6. AECC 7. SEC DSE |
| | THEORY | | | | | | | | |
| 1. | MMT 113 | NUMERICAL ANALYSIS WITH MATLAB | 4 | 0 | - | 4 | 4 | CO-REQUISITE | CC |
| 2. | MMT 106 | COMPLEX ANALYSIS | 4 | 0 | - | 4 | 4 | CO-REQUISITE | CC |
| 3. | MMT 107 | TOPOLOGY | 4 | 0 | - | 4 | 4 | CO-REQUISITE | CC |
| 4. | MMT 108 | DIFFERENTIAL GEOMETRY & TENSOR ANALYSIS | 4 | 0 | - | 4 | 4 | CO-REQUISITE | CC |
| 5. | ENP 601 | TECHNICAL PRESENTATION | - | 0 | 4 | 2 | 2 | CO-REQUISITE | SEC |
| | PRACTICALS | | | | | | | | |
| 6. | MMT 152 | MATHEMATICS LAB- II | - | - | 3 | 3 | 2 | CO-REQUISITE | AECC |
| TOTAL | | | 16 | - | 7 | 21 | 20 | | |

² CC: Core Course, AECC: Ability Enhancement Compulsory Courses, SEC: Skill Enhancement Courses, DSE: Discipline Specific Courses

Department of Mathematics
School of Basic Sciences & Research
M. Sc. (Mathematics)
Batch: 2018-2020

TERM: III

| S. No. | SUBJECT CODE | Title of Paper | HOURS | | | | CREDITS | PRE-REQUISITE/ CO-REQUISITE | Type of Course: 1. CC 2. AECC 3. SEC 4. DSE |
|--------------|-----------------------------|--|-----------|----------|----------|--------------|-----------|-----------------------------|---|
| | THEORY | | L | T | P | TOTAL | | | |
| 1. | MMT-201 | ABSTRACT ALGEBRA | 4 | - | - | 4 | 4 | CO-REQUISITE | CC |
| 2 | MMT 203 | LINEAR PROGRAMMING | 4 | - | - | 4 | 4 | CO-REQUISITE | CC |
| | | SPECIALIZATION PAPERS (I & II)(OPT ANY TWO COURSES) | | | | | | | |
| 3. | MMT 209 / MMT 204 / MMT-206 | Graph Theory and its Applications / FLUID DYNAMICS / NUMBER THEORY WITH CRYPTOGRAPHY | 4+ 4 | - | - | 8 | 8 | CO-REQUISITE | AECC |
| | PRACTICALS | | | | | | | | |
| 4. | MMT 251 | MATHEMATICS LAB- III | - | - | 3 | 3 | 2 | CO-REQUISITE | AECC |
| | DISSERTATION | | | | | | | | |
| 5. | MMT 252 | DISSERTATION-I (A topic from specialization papers) | - | - | | 2 | 2 | CO-REQUISITE | AECC |
| TOTAL | | | 16 | - | 3 | 21 | 20 | | |

³ CC: Core Course, AECC: Ability Enhancement Compulsory Courses, SEC: Skill Enhancement Courses, DSE: Discipline Specific Courses

Department of Mathematics
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M. Sc. (Mathematics)
Batch: 2018-2020

TERM: IV

| S. No. | SUBJECT CODE | Title of Paper | HOURS | | | | CREDITS | PRE-REQUISITE/ CO-REQUISITE | Type of Course4: 1. CC 2. AECC 3. SEC 4. DSE |
|--------------|----------------------------------|--|----------|----------|----------|-----------|-----------|--------------------------------|--|
| | | | L | T | P | TOTAL | | | |
| | THEORY | | | | | | | | |
| | | SPECIALIZATION PAPERS (I & II)(OPT ANY TWO COURSES) | | | | | | | |
| 1. | MST 205 / MMT202 / MMT 208 | FUNCTIONAL ANALYSIS / Measure Theory/ DISCRETE MATHEMATICS | 4+ 4 | - | - | 8 | 8 | CO-REQUISITE | CC |
| | PRACTICALS | ---- | - | - | - | ---- | ---- | ---- | ---- |
| | DISSERTATION | | | | | | | | |
| 2. | MMT 253 | DISSERTATION-2 (A topic from specialization papers) | - | - | | 8 | 8 | CO-REQUISITE | AECC |
| TOTAL | | | 8 | - | - | 16 | 16 | | |

⁴ CC: Core Course, AECC: Ability Enhancement Compulsory Courses, SEC: Skill Enhancement Courses, DSE: Discipline Specific Courses

| | | |
|----------------------------|-----------------------|---|
| School: SBSR | | Batch : 2018-20 |
| Program: M.Sc. | | Current Academic Year: 2018-19 |
| Branch: Mathematics | | Semester: I |
| 1 | Course Code | MMT 101 |
| 2 | Course Title | Real Analysis |
| 3 | Credits | 4 |
| 4 | Contact Hours (L-T-P) | 4-0-0 |
| | Course Status | Compulsory |
| 5 | Course Objective | <p>1. The objective of this course is to develop the knowledge of various concepts of Real numbers and their properties.</p> <p>2. The objective of this course is to develop a deeper and more rigorous understanding of Calculus including defining terms and proving theorems about sequences, series, limits, continuity, derivatives, the Riemann integrals, and sequences of functions.</p> |
| 6 | Course Outcomes | <p>CO1: Explain functions between sets; equivalent sets; finite, countable and uncountable sets and some operations on real numbers. (K2,K4)</p> <p>CO2: Evaluate convergent, divergent, bounded, Cauchy and monotone sequences and series. (K2,K5)</p> <p>CO3: Explain and determine the continuity, discontinuity and uniform continuity of functions. (K2,K3,K4)</p> <p>CO4: Determine the uniform convergence of sequences and series. (K2,K3)</p> <p>CO5: Evaluate convergence and divergence of sequences and series of functions. (K2,K5)</p> <p>CO6: Describe and use the concepts of fundamental theorem of Integral calculus, Riemann Integral and Riemann – Stieltjes integral (K2,K3)</p> |
| 7 | Course Description | This course is an introduction to the fundamentals of Real analysis. This provides the understanding of convergence, divergence, uniform convergence and absolute convergence of sequences and series of Real numbers. It gives an idea about continuity, discontinuity and uniform continuity of functions. It will be helpful in solving Real integrals. |
| 8 | Outline syllabus | Real analysis |
| | Unit 1 | |
| | A | Neighbourhoods of a point in \mathbb{Y} , open and closed intervals in \mathbb{Y} , neighbourhoods of points in \mathbb{Y}^2 |
| | B | limit points of sets, compact sets of \mathbb{R} |
| | C | Bolzano-Weierstrass theorem, Heine-Borel theorem |
| | Unit 2 | |
| | A | Sequence of real numbers, convergence of sequences |
| | B | Cauchy sequence, limit superior and limit inferior of sequences |
| | | CO Mapping |

Beyond Boundaries

| | | | | | | | | | |
|-----|------------------------|--|-----|-----|-----|-----|-----|-----|--|
| | C | Series – convergence, tests of convergence, conditional and absolute convergence | CO2 | | | | | | |
| | Unit 3 | | | | | | | | |
| | A | Continuous functions, uniform and absolute continuity | CO3 | | | | | | |
| | B | uniform convergence of sequences and series | CO4 | | | | | | |
| | C | Term by term differentiation, power series | CO4 | | | | | | |
| | Unit 4 | | | | | | | | |
| | A | Sequences and series of functions, point-wise and uniform convergence, Cauchy criterion for uniform convergence | CO5 | | | | | | |
| | B | Weierstrass M test, Abel’s and Dirichlet’s test for uniform convergence and differentiation, uniform convergence and integration, Weierstrass approximation theorem | CO5 | | | | | | |
| | C | Power series, uniqueness theorem of power series, Abel’s and Taylor’s theorem, rearrangement of terms of series, Riemann’s theorem | CO5 | | | | | | |
| | Unit 5 | | | | | | | | |
| | A | The fundamental theorem of integral calculus, definition of Riemann integral, refinement of partitions, Darboux’s theorem | CO6 | | | | | | |
| | B | Properties and some important theorems on Riemann integral, integration of vector valued functions, | CO6 | | | | | | |
| | C | Riemann – Stieltjes integral, refinement of partitions, properties and some important theorems on Riemann – Stieltjes integration | CO6 | | | | | | |
| | Mode of examination | Theory | | | | | | | |
| | Weightage Distribution | <table><tr><td>CA</td><td>MTE</td><td>ETE</td></tr><tr><td>30%</td><td>20%</td><td>50%</td></tr></table> | CA | MTE | ETE | 30% | 20% | 50% | |
| CA | MTE | ETE | | | | | | | |
| 30% | 20% | 50% | | | | | | | |
| | Text book/s* | <div>1. Jain P. K. and Gupta V. P.: Lebesgue measure and integration, Wiley Eastern Ltd., New Age Int. Ltd., New Delhi, (1994).</div> <div>2. Rudin W.: Principles of Mathematical Analysis</div> | | | | | | | |
| | Other References | <div>(i) Malik S. C. and Savita Arora; Mathematical Analysis, second ed., Wiley Eastern Ltd., New Age Int. Ltd., New Delhi, (1994).</div> <div>(ii) Somasundaram D. and Chaudhary B.: A first course of Mathematical Analysis, Narosa publishing house, New Delhi, 1987.</div> | | | | | | | |

COURSE OUTCOMES (CO's) – PROGRAMME OUTCOMES (PO's) MAPPING

TABLE

| PO | PO1 | PO2 | PO3 | PO4 | PO5 | PSO1 | PSO2 | PSO3 | PSO4 |
|---------------|----------|----------|----------|----------|----------|----------|----------|----------|----------|
| CO | | | | | | | | | |
| C101.1 | 3 | 3 | 3 | 3 | 3 | 3 | 3 | 2 | 1 |
| C101.2 | 3 | 2 | 3 | 3 | 2 | 3 | 2 | 1 | 1 |
| C101.3 | 2 | 2 | 2 | 2 | 2 | 2 | 2 | 1 | 1 |
| C101.4 | 2 | 2 | 1 | 2 | 2 | 2 | 3 | 1 | 1 |
| C101.5 | 3 | 2 | 2 | 3 | 2 | 3 | 2 | 2 | 2 |
| C101.6 | 3 | 2 | 1 | 3 | 2 | 2 | 2 | 1 | 2 |

| | | |
|----------------------------|-----------------------|---|
| School: SBSR | | Batch : 2018-20 |
| Program: M.Sc. | | Current Academic Year: 2018-19 |
| Branch: Mathematics | | Semester: I |
| 1 | Course Code | MMT102 |
| 2 | Course Title | LINEAR ALGEBRA |
| 3 | Credits | 4 |
| 4 | Contact Hours (L-T-P) | 4-0-0 |
| | Course Status | Compulsory |
| 5 | Course Objective | <p>1. To familiarise students with basic concept of determinants, properties of determinants, rank of a matrix, inverse of a non-singular square Matrix, solution of system of linear equations. Have an idea of the fields and vector spaces, linear transformations, null spaces, rank and nullity theorem, inner products and norms, orthogonal vectors, Cauchy-Schwarz inequality, Orthogonal bases, Gram - Schmidt process.</p> <p>2. Have an understanding of Characteristic roots of real matrices, right and left characteristic vectors, independence of characteristic vectors corresponding to distinct characteristic roots. To know definiteness of a real quadratic form, simultaneous reduction of two quadratic forms, maxima and minima of ratio of two quadratic forms.</p> |

| | | |
|---|-------------------------|---|
| 6 | Course Outcomes | <p>CO1: Describe the basic concept of determinants, properties of determinants, and solve rank of a matrix, inverse of a non-singular square matrix and evaluate solution of system of linear equations. (K1,K2,K3,K5)</p> <p>CO2: Describe the concept of fields and vector spaces, linear transformations, null spaces, explain rank and nullity theorem. (K1,K2, K4)</p> <p>CO3: Explain the concept of inner products and norms, orthogonal vectors, Cauchy-Schwarz inequality and evaluate orthogonal bases, define Gram - Schmidt process. (K1, K2, K4, K5)</p> <p>CO4: Explain characteristic roots of real matrices, right and left characteristic vectors and evaluate independence of characteristic vectors corresponding to distinct characteristic roots. (K2, K4, K5)</p> <p>CO5: Illustrate generalized inverse of a matrix, left inverse, right inverse and pseudo inverse and compose Spectral decomposition theorem. (K3, K6)</p> <p>CO6: Explain Definiteness of a real quadratic form, simultaneous reduction of two quadratic forms and evaluate maxima and minima of ratio of two quadratic forms. (K2, K4, K5)</p> |
| 7 | Course Description | This course is an introduction to Linear Algebra. The primary objective of the course is to develop the advance understanding of linear algebra. |
| 8 | Outline syllabus | LINEAR ALGEBRA |
| | | CO Mapping |
| | Unit 1 | Review of Matrix Algebra |
| | A | Determinants, properties of determinants |
| | B | rank of a matrix, inverse of a non-singular square Matrix |
| | C | Solution of system of linear equations. |
| | Unit 2 | Vector Spaces |
| | A | Fields and vector spaces, linear transformations, null spaces, rank and nullity theorem, |
| | B | Inner products and norms, orthogonal vectors, Cauchy-Schwarz inequality, |
| | C | Orthogonal bases, Gram - Schmidt process |
| | Unit 3 | Characteristic roots and Characteristic Vectors |
| | A | Characteristic roots of real matrices |
| | B | Right and left characteristic vectors, |
| | C | Independence of characteristic vectors corresponding to distinct characteristic roots |
| | Unit 4 | Generalized Inverse |
| | A | Generalized inverse of a matrix |
| | B | Left inverse, right inverse and pseudo inverse |
| | C | Applications, Spectral decomposition theorem. |
| | Unit 5 | Quadratic Forms |
| | A | Definiteness of a real quadratic form |
| | B | Simultaneous reduction of two quadratic forms, |
| | C | Maxima and minima of ratio of two quadratic forms. |

| | | | | | |
|--|------------------------|--|-----|-----|--|
| | Mode of examination | Theory | | | |
| | Weightage Distribution | CA | MTE | ETE | |
| | | 30% | 20% | 50% | |
| | Text book/s* | 1. Graybill F.A.: Matrix with applications in statistics, 2nd Ed., Wadsworth (1983). 2. Rao C. R. & Mitra S. K. : Generalized inverse of matrices and its application. John Wiley & Sons Inc. (1971) | | | |
| | Other References | 3. Kenneth Hoffman & Ray Kunze: Linear Algebra, EEE, PHI learning (Indian Ed.), 2012. 4. Hohn F. E.: Elements of Matrix Algebra, Macmillan, (1973). 5. Searle S. R.: Matrix Algebra useful to statistics, John Willey & Sons 1982. | | | |

COURSE OUTCOMES – PROGRAMME OUTCOMES MAPPING TABLE

| PO | PO1 | PO2 | PO3 | PO4 | PO5 | PSO1 | PSO2 | PSO3 | PSO4 |
|---------------|----------|----------|----------|----------|----------|----------|----------|----------|----------|
| CO | | | | | | | | | |
| C102.1 | 3 | 3 | 3 | 3 | 3 | 3 | 3 | 2 | 1 |
| C102.2 | 3 | 2 | 3 | 3 | 2 | 3 | 2 | 1 | 2 |
| C102.3 | 2 | 2 | 2 | 2 | 2 | 2 | 2 | 2 | 1 |
| C102.4 | 2 | 2 | 1 | 2 | 2 | 2 | 3 | 1 | 2 |
| C102.5 | 3 | 2 | 2 | 3 | 2 | 3 | 2 | 2 | 1 |
| C102.6 | 3 | 2 | 1 | 3 | 3 | 2 | 2 | 1 | 1 |

| | | |
|----------------------------|-----------------------|--|
| School: SBSR | | Batch : 2018-20 |
| Program: M. Sc. | | Current Academic Year: 2018 - 19 |
| Branch: Mathematics | | Semester: I |
| 1 | Course Code | MMT 105 |
| 2 | Course Title | ORDINARY AND PARTIAL DIFFERENTIAL EQUATIONS |
| 3 | Credits | 4 |
| 4 | Contact Hours (L-T-P) | 4-0-0 |
| | Course Status | Compulsory |
| 5 | Course Objective | <ul style="list-style-type: none"> Familiarise students with basic concepts of ordinary and partial differential equations and learn to solve first-order ordinary differential equations and formation of ODEs. Explore the methods to solve Linear differential equation of nth order with constant coefficients and variable coefficients. Students will also master the technique of separation of variables to solve PDEs and able to derive heat and wave equations |
| 6 | Course Outcomes | <p>CO1: Explain and illustrate how to form the ordinary differential equations and solve the equations of first order and first degree. (K2,K3,K4)</p> <p>CO2: Describe and solve the linear differential equation of nth order with constant coefficients. (K1, K2, K3)</p> <p>CO3: Explain Cauchy Euler's equations and solve the same, evaluate simultaneous linear differential equations by method of variation of parameters. (K2,K3,K4,K5)</p> <p>CO4: Describe the classification of PDEs of second order and evaluate the wave equation by using method of separation of variable. (K1,K2,K5)</p> <p>CO5: Evaluate the heat equation in one dimension in various cases. (K5)</p> <p>CO6: Explain and then evaluate Laplace equation. (K2, K4, K5)</p> |
| 7 | Course Description | This course is an introduction to ordinary and partial differential equations. The primary objective of the course is to develop the advance understanding of ordinary and partial differential equations. |
| 8 | Outline syllabus | CO Mapping |
| | Unit 1 | |
| | A | Basics of differential equations including order, degree, type of differential equation and formation of differential equations. |
| | B | Equations of first order and first degree including separation of variables, homogeneous and exact differential equations (including integrating factor). |
| | C | Linear differential equations. |
| | Unit 2 | |
| | A | Linear differential equation of nth order with constant coefficients, auxiliary equations |
| | B | auxiliary equations, complementary functions |

| | | | | | |
|--|------------------------|---|-----|-----|-----|
| | C | particular integrals for various standard functions and their combinations | | | CO2 |
| | Unit 3 | | | | |
| | A | Cauchy Euler’s equations and equations reducible to homogeneous form | | | CO3 |
| | B | Simultaneous linear differential equations | | | CO3 |
| | C | method of variation of parameters | | | CO3 |
| | Unit 4 | | | | |
| | A | Classification of PDEs of second order, Boundary value problems, the principle of superposition | | | CO4 |
| | B | method of separation of variables, its application to solve wave equation | | | CO4 |
| | C | D’Alembert’s solution of wave equation in various cases.. | | | CO4 |
| | Unit 5 | | | | |
| | A | Solution of heat equation in one dimension in various cases | | | CO5 |
| | B | solution of Laplace equation in Cartesian coordinates | | | CO6 |
| | C | its conversion into polar coordinates. | | | CO6 |
| | Mode of examination | Theory/Jury/Practical/Viva | | | |
| | Weightage Distribution | CA | MTE | ETE | |
| | | 30% | 20% | 50% | |
| | Text book/s* | 1. Ordinary and Partial Differential equations by M. D. Raisinghania, S Chand and Company Ltd. 2. Schaum’s Outline Series of Partial Differential equations 3. Schaum’s Outline Series of Ordinary Differential equations . | | | |
| | Other References | 1. An introduction to Ordinary Differential Equations by Earl. A. Codington, DOVER PUBLICATIONS, INC. New York. 2. Elements of Partial Differential Equations by Ian N. Sneddon, McGRA-HILL Book Company. | | | |

COURSE OUTCOMES – PROGRAMME OUTCOMES MAPPING TABLE

| PO | PO1 | PO2 | PO3 | PO4 | PO5 | PSO1 | PSO2 | PSO3 | PSO4 |
|---------------|----------|----------|----------|----------|----------|----------|----------|----------|----------|
| CO | | | | | | | | | |
| C105.1 | 3 | 3 | 3 | 3 | 3 | 3 | 3 | 2 | 1 |
| C105.2 | 3 | 2 | 3 | 3 | 2 | 3 | 2 | 1 | 2 |
| C105.3 | 2 | 2 | 3 | 2 | 2 | 2 | 3 | 2 | 1 |
| C105.4 | 2 | 2 | 1 | 2 | 2 | 2 | 3 | 1 | 2 |
| C105.5 | 3 | 2 | 2 | 3 | 2 | 3 | 2 | 2 | 2 |
| C105.6 | 3 | 2 | 1 | 3 | 2 | 2 | 2 | 2 | 2 |

| | | |
|----------------------------|-----------------------|--|
| School: SBSR | | Batch : 2018-20 |
| Program: M. Sc. | | Current Academic Year: 2018 - 19 |
| Branch: Mathematics | | Semester: I |
| 1 | Course Code. | MMT104 |
| 2 | Course Title | STATISTICAL METHODS |
| 3 | Credits | 4 |
| 4 | Contact Hours (L-T-P) | 4-0-0 |
| | Course status | Compulsory |
| 5 | Course Objectives | <ul style="list-style-type: none"> To familiarise the students how to calculate and apply measures of location and measures of dispersion --grouped and ungrouped data cases and communicate quantitative data verbally, graphically, symbolically and numerically. To make students familiar with the concept of Probability and Statistics, discrete and continuous probability distributions to various business problems and theory of measure theory and integration of a measurable function with respect to a measure |
| 6 | Course Outcomes | CO1: Describe the overall process and particular steps in designing studies, collecting and analyzing data, interpreting and presenting results; Develop skills in presenting quantitative data using appropriate diagrams, tabulations and summaries. (K1, K2, K6) CO2: Explain the basic concepts of probability, random variables, probability |

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| | | <p>distribution, and joint probability distribution and describe the properties of discrete and continuous distribution functions. (K1,K2,K4)</p> <p>CO3: Explain the fundamentals of measure theory and be acquainted with the proofs of the fundamental theorems underlying the theory of integration and illustrate measure theory random variables, independence, expectations and conditional expectations, product measures and discrete parameter martingales. (K2,K3,K4)</p> <p>CO4: Explain the concept of length, area, volume using lebesgue's theory. (K2,K4)</p> <p>CO5: Describe how these underpin the use of Mathematical concepts such as volume, area, and integration and evaluate the same. (K1,K2, K5)</p> <p>CO6: Explain and illustrate the general principles of measure theory and integration in such concrete subjects as the theory of probability. (K2,K3,K4)</p> |
| 7 | Course Description | In this course we will explore the use of statistical methodology in designing, analyzing, interpreting, and presenting experiments and observations. We will cover descriptive statistics, probability, discrete random variables, continuous random variables, probability distributions and also learn the basic elements of Measure Theory, with related discussions on applications in probability theory. |
| 8 | Outline syllabus: | |
| UNIT 1 | Descriptive Statistics and Probability | CO Mapping |
| A | Representation of data (measures of central tendency). | CO1 |
| B | Dispersion & other characteristics of data (mean deviation, variance, quartiles, Skewness and Kurtosis, Moments). | CO1 |
| C | probability (elementary theorems, Baye's theorem). | CO1 |
| UNIT 2 | Random variable and Probability Distribution | |
| A | Random variables, expectation, variance, mean, median, mode, moments, moment generating function. | CO2 |
| B | Special discrete & continuous distributions and their mean & variance. | CO2 |
| C | Binomial, poisson, exponential, Gamma, normal, t, Chi-square, F distributions, simple applications. | CO2 |
| UNIT 3 | Probability measure | |
| A | Classes of sets, fields, sigma fields, lim sup, liminf of sequences of sets. | CO3 |
| B | Measure, probability measure, properties of measure. | CO3 |
| C | Caratheodory extension theorem (only statement), Lebesgue measure. | CO3, CO4 |
| UNIT 4 | Measurable functions | |
| A | Measurable functions, sequence of random variables. | CO3, CO5 |
| B | Almost sure convergence. | CO5,CO6 |
| C | Convergence in probability and measure. | CO5,CO6 |
| UNIT 5 | Integration | |
| A | Integration of a measurable function with respect to a measure. | CO5,CO6 |

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|---|---|--|-----|---------|
| B | Monotone convergence theorem. | | | CO5,CO6 |
| C | Fatou's lemma, dominated convergence theorem. | | | CO5,CO6 |
| | Mode of Examination | Theory | | |
| | Weightage distribution | CA | MTE | ETE |
| | | 30% | 20% | 50% |
| | Text books | 1. Gupta,S.C and Kapoor,V.K, "Fundamental of Mathematical Statistics". Sultan Chand & sons. | | |
| | Other references | 1. ROBERT A.: Real analysis and probability, Academic Press (1972). 2. BILLINGSLY P.: Probability and measure, Willey (1989). 3. KINGMAN J.-F. C. & TAYLOR S. J.: Introduction to measure and probability, Cambridge university press. | | |

COURSE OUTCOMES – PROGRAMME OUTCOMES MAPPING TABLE

| PO | PO1 | PO2 | PO3 | PO4 | PO5 | PSO1 | PSO2 | PSO3 | PSO4 |
|---------------|----------|----------|----------|----------|----------|----------|----------|----------|----------|
| CO | | | | | | | | | |
| C104.1 | 3 | 3 | 3 | 3 | 3 | 3 | 3 | 2 | 1 |
| C104.2 | 3 | 2 | 3 | 3 | 2 | 3 | 2 | 1 | 2 |
| C104.3 | 2 | 2 | 2 | 2 | 2 | 2 | 2 | 2 | 1 |
| C104.4 | 2 | 2 | 1 | 2 | 2 | 2 | 3 | 1 | 1 |
| C104.5 | 3 | 2 | 2 | 3 | 2 | 3 | 2 | 2 | 2 |
| C104.6 | 3 | 2 | 1 | 3 | 2 | 2 | 2 | 1 | 2 |

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|----------------------------|-----------------------|--|
| School: SBSR | | Batch : 2018-20 |
| Program: M.Sc. | | Current Academic Year: 2018-19 |
| Branch: Mathematics | | Semester: I |
| 1 | Course Code | MMT-119 |
| 2 | Course Title | INTRODUCTION TO MATLAB AND ITS APPLICATIONS |
| 3 | Credits | 3 |
| 4 | Contact Hours (L-T-P) | 3-0-0 |
| | Course Status | Compulsory |
| 5 | Course Objective | The goal of this course is to introduce the necessary mathematical concepts for MATLAB and cover the syntax and semantics of MATLAB including control structures, comments, variables, functions etc. Once the foundations of the language have been established students will explore different types of scientific programming problems including curve fitting, ODE solving etc. |
| 6 | Course Outcomes | CO1: Describe the fundamentals of MATLAB and use MATLAB for interactive computations. (K2, K3) CO2: Demonstrate with strings and matrices and their uses. (K2, K3) CO3: Illustrate basic flow controls (if-else, for, while). (K3) CO4: Create plots and export this for use in reports and presentations. (K3, K5) CO5: Develop program scripts and functions using the MATLAB development environment. (K4, K5) CO6: Write the program for evaluates linear system of equations, ordinary differential equations in MATLAB. (K5,K6) |
| 7 | Course Description | The course will give the fundamental knowledge and practical abilities in MATLAB required to effectively utilize this tool in technical numerical computations and visualisation in other courses. Syntax and interactive computations, programming in MATLAB using scripts and functions, rudimentary algebra and analysis. One- and two-dimensional graphical presentations. Examples on engineering applications. |
| 8 | Outline syllabus | Introduction to MATLAB |
| | Unit 1 | Introduction |
| | A | Vector and matrix generation, Subscripting and the colon notation. |
| | B | Matrix and array operations and their manipulations, |
| | C | Introduction to some inbuilt functions. |
| | Unit 2 | Relational and Logical Operators |
| | A | Flow control using various statement and loops including If-End statement, If-Else –End statement |
| | B | Nested If-Else-End Statement, |
| | C | For – End and While-End loops with break commands. |
| | | CO Mapping |

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| | Unit 3 | m-files | |
| | A | Scripts and functions | CO2,CO5 |
| | B | concept of local and global variable | CO2,CO5 |
| | C | Few examples of in-built functions, editing, saving m-files. | CO2,CO5 |
| | Unit 4 | Two dimensional Graphics | |
| | A | Basic Plots, Change in axes and annotation in a figure | CO4 |
| | B | multiple plots in a figure | CO4 |
| | C | saving and printing figures | CO4 |
| | Unit 5 | Applications of MATLAB | |
| | A | Solving a linear system of equations, | CO5, CO6 |
| | B | Curve fitting with polynomials using inbuilt function such as polyfit, solving equations in one variable, | CO5, CO6 |
| | C | Solving ordinary differential equations using inbuilt functions | CO5, CO6 |
| | Mode of examination | Theory | |
| | Weightage Distribution | CA 30% | MTE 20% |
| | | | ETE 50% |
| | Text book | An introduction to MATLAB : Amos Gilat | |
| | Other References | 1. Applied Numerical Methods with Matlab for engineering and Scientists by stevenchapra, Mcgraw Hill. 2. Getting started with Matlab: RudraPratap | |

COURSE OUTCOMES – PROGRAMME OUTCOMES MAPPING TABLE

| PO | PO1 | PO2 | PO3 | PO4 | PO5 | PSO1 | PSO2 | PSO3 | PSO4 |
|---------------|----------|----------|----------|----------|----------|----------|----------|----------|----------|
| CO | | | | | | | | | |
| C119.1 | 3 | 3 | 3 | 3 | 3 | 3 | 3 | 2 | 1 |
| C119.2 | 3 | 2 | 3 | 3 | 2 | 3 | 2 | 1 | 2 |
| C119.3 | 2 | 2 | 2 | 2 | 2 | 2 | 2 | 1 | 1 |
| C119.4 | 2 | 2 | 1 | 2 | 2 | 2 | 3 | 1 | 1 |
| C119.5 | 3 | 2 | 2 | 3 | 2 | 3 | 2 | 2 | 2 |
| C119.6 | 3 | 2 | 1 | 3 | 2 | 2 | 2 | 1 | 2 |

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|----------------------------|-----------------------|---|
| School: SBSR | | Batch : 2018-20 |
| Program: M.Sc. | | Current Academic Year: 2018-19 |
| Branch: Mathematics | | Semester: II |
| 1 | Course Code | MMT-123 |
| 2 | Course Title | NUMERICAL ANALYSIS WITH MATLAB |
| 3 | Credits | 4 |
| 4 | Contact Hours (L-T-P) | 4-0-0 |
| | Course Status | Compulsory |
| 5 | Course Objective | <ul style="list-style-type: none"> To provide the student with numerical methods of solving the non-linear equations, interpolation, differentiation, and integration. To improve the student's skills in numerical methods by using the MATLAB |
| 6 | Course Outcomes | <p>CO1: Calculate the error and evaluate the floating point and develop the algorithm in MATLAB. (K1,K3,K5,K6)</p> <p>CO2: Solve a linear system of equations using an appropriation method and develop the algorithm in MATLAB. (K1,K,K5,K6)</p> <p>CO3: Solve the algebraic or transcendental equations using numerical methods and develop the algorithm in MATLAB. (K1,K3,K5,K6)</p> <p>CO4: Calculate a definite integral using an appropriation method and develop the algorithm in MATLAB. (K1,K3,K5,K6)</p> <p>CO5: Derivations and stability analysis for Taylor series method.</p> <p>CO6: Evaluate differential equation by Euler's method and its variants, Runge- Kutta second order and fourth order methods and develop the algorithm in MATLAB. (K1,K3,K5,K6)</p> |
| 7 | Course Description | This course is an introduction to the numerical analysis. The primary objective of the course is to develop the basic understanding of numerical algorithms and skills to implement algorithms to solve mathematical problems in MATLAB. |
| 8 | Outline syllabus | CO Mapping |
| | Unit 1 | Error Analysis: |
| | A | Definition and sources of errors, Propagation of errors |
| | B | Sensitivity and conditioning, Stability and accuracy, |
| | C | Floating-point arithmetic and rounding errors. |
| | Unit 2 | Solution of system of linear equations: |
| | A | Direct methods: Cramer's rule, Matrix inverse method, |
| | B | Gauss elimination and Gauss-Jordan method |
| | C | Iterative methods: Jacobi's method, Gauss-Seidal method |

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| | Unit 3 | System of Transcendental equations | | | |
| | A | Initial approximation of the roots, Bisection method, | | | CO3 |
| | B | Method of false position, secant method, iteration method | | | CO3 |
| | C | Newton-Raphson method and its convergence. | | | CO3 |
| | Unit 4 | Numerical differentiation and integration: | | | |
| | A | Differentiation using Newton's forward and backward formula | | | CO4 |
| | B | Newton-Cotes quadrature formula - derivations | | | CO4 |
| | C | Comparison of Trapezoidal rule, Simpson's 1/3 and 3/8 rules. | | | CO4 |
| | Unit 5 | Initial value Problems | | | |
| | A | Single-step methods: General definitions and Lipschitz condition, Derivations and stability analysis for Taylor series method, | | | CO5 |
| | B | Euler's method and its variants, Runge- Kutta second order and fourth order methods; | | | CO6 |
| | C | Implementation of these methods for various test problems using MATLAB | | | CO6 |
| | Mode of examination | Theory | | | |
| | Weightage Distribution | CA | MTE | ETE | |
| | | 30% | 20% | 50% | |
| | Text book/s* | 1) An Introduction to Numerical Analysis by EndreSuli, David F. Mayers, Cambridge University Press, 2003. 2) Applied Numerical Analysis by C. F. Gerald, Pearson Education, 2009. 3) Elements of Numerical Analysis by R. S. Gupta, Macmillan India Ltd, 2009. | | | |
| | Other References | 1) Numerical methods in Engineering & Science by B. S. Grewal, Khanna Publishers, 2013. 2) Numerical methods for Scientific and Engineering Computation by Jain, Iyengar, Jain, New Age International Publishers, 2004. | | | |

COURSE OUTCOMES – PROGRAMME OUTCOMES MAPPING TABLE

| PO | PO1 | PO2 | PO3 | PO4 | PO5 | PSO1 | PSO2 | PSO3 | PSO4 |
|--------|-----|-----|-----|-----|-----|------|------|------|------|
| CO | | | | | | | | | |
| C123.1 | 3 | 3 | 3 | 3 | 3 | 3 | 3 | 2 | 1 |
| C123.2 | 3 | 2 | 3 | 3 | 2 | 3 | 2 | 1 | 1 |
| C123.3 | 2 | 2 | 2 | 3 | 2 | 2 | 2 | 2 | 2 |
| C123.4 | 2 | 2 | 2 | 3 | 2 | 2 | 3 | 1 | 1 |
| C123.5 | 3 | 2 | 2 | 3 | 2 | 3 | 2 | 2 | 2 |
| C123.6 | 3 | 2 | 1 | 3 | 2 | 2 | 2 | 1 | 2 |

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|----------------------------|-----------------------|---|
| School: SBSR | | Batch : 2018-20 |
| Program: M.Sc. | | Current Academic Year: 2018-2019 |
| Branch: Mathematics | | Semester: II |
| 1 | Course Code | MMT-106 |
| 2 | Course Title | Complex Analysis |
| 3 | Credits | 4 |
| 4 | Contact Hours (L-T-P) | 4-0-0 |
| | Course Status | Compulsory |
| 5 | Course Objective | <ul style="list-style-type: none"> This course is aimed to provide an introduction to the theories for functions of a complex variable. The concepts of analyticity, Cauchy-Riemann relations and harmonic functions, Complex integration and complex power series are presented. Discuss the classification of isolated singularities and examine the theory and illustrate the applications of the calculus of residues in the evaluation of integrals. Students will study geometric properties of conformal mappings in the plane and their relations with analytic functions |
| 6 | Course Outcomes | CO1: Discuss the concept of complex number and its algebra calculates continuity, differentiability, analyticity of a function and analyse the derivative of a function. (K2,K3, K4) CO2: Describe the concept of analytic function and check the analyticity of the functions. (K3, K6) CO 3: Explain the concept of harmonic function and evaluate |

Beyond Boundaries

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| | | <p>harmonic conjugates and discuss about series and their convergence, power series, radius of convergence. (K2, K4,K5)</p> <p>CO 4: Illustrate the concept of complex integration, write the Green's theorem, anti-derivative theorem, Cauchy-Goursat theorem, Cauchy's integral formula, Liouville theorem, Morera's theorem and evaluate derivative of analytic functions. (K3, K5,K6)</p> <p>CO 5: Discuss the concept of singularities and its types; write Taylor and Laurent series, Cauchy's residue theorem, evaluate the definite integrals using Cauchy's residue theorem.(K1,K2,K5,K6)</p> <p>CO6: Demonstrate the understanding of conformal mappings and Construct conformal mappings between many kinds of domain. (K2, K5)</p> | |
| 7 | Course Description | This course is an introduce the theories for functions of a complex variable. The concepts of analyticity, Cauchy-Riemann relations and harmonic functions, Complex integration and complex power series are presented. Discuss the classification of isolated singularities and examine the theory and illustrate the applications of the calculus of residues in the evaluation of integrals. | |
| 8 | Outline syllabus | | CO Mapping |
| | Unit 1 | | |
| | A | Complex numbers, their representation in Argand's plane and the algebra of complex numbers, | CO1 |
| | B | The complex plane and open set, domain and region in a complex plane | CO1 |
| | C | Complex functions and their limits, continuity, differentiability. | CO1 |
| | Unit 2 | | |
| | A | Analytic function, The C-R equations and sufficient conditions for differentiability and analyticity | CO2 |
| | B | Harmonic functions and harmonic conjugates, Sequences, | CO3 |
| | C | Series and their convergence, power series, radius of convergence. | CO3 |
| | Unit 3 | | |
| | A | Complex integration: Line integration, path independence, | CO4 |
| | B | Green's theorem, anti-derivative theorem, Cauchy-Goursat theorem, Cauchy's integral formula, | CO4 |
| | C | Derivative of analytic functions, Liouville theorem, Morera's theorem. | CO4 |
| | Unit 4 | | |
| | A | Singularities and its types; Taylor and Laurent series | CO5 |
| | B | Cauchy's residue theorem, | CO5 |
| | C | Evaluation of definite integrals using Cauchy's residue theorem. | CO5 |
| | Unit 5 | | |

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| | A | Transformations or mappings, some standard transformations, | | | CO6 |
| | B | Bilinear transformation, fixed point of a transformation, | | | CO6 |
| | C | Conformal transformation, jacobian of a transformation and few special conformal mappings | | | CO6 |
| | Mode of examination | Theory | | | |
| | Weightage Distribution | CA | MTE | ETE | |
| | | 30% | 20% | 50% | |
| | Text book/s* | 1) Churchill, Ruel V. and Brown, James Ward, Complex Variables and Applications, fourth edition, McGraw-Hill Book Co., New York, 1984. 2) Conway, John B., Functions of One Complex Variable, II, Graduate Texts in Mathematics, 159, Springer-Verlag, New York, 1995. | | | |
| | Other References | 1) Schaum's Outline of Complex Variables, 2ed by By Murray Spiegel, Seymour Lipschutz, John Schiller, Dennis Spellman 2) Ahlfors, Lars V., Complex Analysis: An Introduction to the Theory of Analytic Functions of One Complex Variable, third edition. International Series in Pure and Applied Mathematics, McGraw-Hill Book Co., New York, 1978. | | | |

COURSE OUTCOMES – PROGRAMME OUTCOMES MAPPING TABLE

| PO | PO1 | PO2 | PO3 | PO4 | PO5 | PSO1 | PSO2 | PSO3 | PSO4 |
|---------------|-----|-----|-----|-----|-----|------|------|------|------|
| CO | | | | | | | | | |
| C106.1 | 3 | 3 | 3 | 3 | 3 | 3 | 3 | 2 | 1 |
| C106.2 | 3 | 2 | 3 | 3 | 2 | 3 | 2 | 1 | 1 |
| C106.3 | 2 | 2 | 3 | 2 | 2 | 2 | 3 | 2 | 2 |
| C106.4 | 2 | 2 | 2 | 2 | 2 | 2 | 3 | 1 | 1 |
| C106.5 | 3 | 2 | 2 | 3 | 2 | 3 | 2 | 2 | 2 |
| C106.6 | 3 | 2 | 1 | 3 | 2 | 2 | 2 | 1 | 2 |

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|----------------------------|-----------------------|---|------------|
| School: SBSR | | Batch : 2018-20 | |
| Program: M.Sc. | | Current Academic Year: 2018-2019 | |
| Branch: Mathematics | | Semester: II | |
| 1 | Course Code | MMT 107 | |
| 2 | Course Title | TOPOLOGY | |
| 3 | Credits | 4 | |
| 4 | Contact Hours (L-T-P) | 4-0-0 | |
| | Course Status | Compulsory | |
| 5 | Course Objective | This course provides an introduction to topics involving concepts of Topological space and separate axioms (Hausdorff space and base problems), Compactness (Urysohn's theorem), Connectedness With Nets (converge filter Zorn's lemma). | |
| 6 | Course Outcomes | <p>CO1: Explain the concept of Topological spaces and calculate interior, exterior limit point and boundary points. (K2, K3, K4)</p> <p>CO2: Describe the concept of separate axioms and evaluate T_0, T_1, T_2 spaces, normal and completely normal spaces. (K1, K2, K5)</p> <p>CO3: Discuss the compactness (Urysohn's theorem) and evaluate cover, open cover, finite sub cover, compact sets. (K1, K2, K5)</p> <p>CO4: Explain Lindeloff space, locally compact, Map: continuous function and write Heine borel theorem, describe homeomorphism, open and closed map, compactness for continuous images. (K2, K4, K6)</p> <p>CO5: Explain about separated sets, disconnectedness, totally disconnectedness, maximal connected set and illustrate component and path, locally connected and write Urysohn's theorem. (K2, K3, K4, K6)</p> <p>CO6: Describe the concept of Nets and Filters and write zorn's lemma. (K1, K2, K6)</p> | |
| 7 | Course Description | This course provides an introduction to topics involving concepts of Topological space and separate axioms (Hausdorff space and base problems), Compactness (Urysohn's theorem), Connectedness With Nets (converge filter Zorn's lemma). The primary objective of the course is to develop the advance understanding of Topology. | |
| 8 | Outline syllabus | | CO Mapping |
| | Unit 1 | Topological space | |
| | A | Topology, weaker and stronger topology, indiscrete and discrete topology | CO1 |
| | B | Co-finite and usual topology, interior, exterior | CO1 |
| | C | limit point and boundary points. | CO1 |
| | Unit 2 | Separation axioms | |
| | A | Base, sub-base and countability (first countable and second countable) | CO2 |

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| | B | separation axioms: T_0, T_1, T_2 spaces, normal and completely normal spaces | | | CO2 |
| | C | regular and completely regular spaces, T_3, T_4 and Tychonoff space, Hausdorff space and based problems | | | CO2 |
| | Unit 3 | Compactness | | | |
| | A | Cover, open cover, finite sub cover, compact sets, finite intersection property | | | CO3 |
| | B | Heine borel theorem, Lindeloff space, locally compact, Map: continuous function | | | CO3, CO4 |
| | C | homeomorphism, open and closed map, compactness for continuous images | | | CO3, CO4 |
| | Unit 4 | Connectedness | | | |
| | A | Separated sets, disconnectedness, totally disconnectedness, maximal connected set | | | CO5 |
| | B | component and path, locally connected and based examples | | | CO5 |
| | C | Urysohn's theorem (proof). | | | CO5 |
| | Unit 5 | Nets | | | |
| | A | Binary relation, Directed set, residual subset, sequence convergence of a set | | | CO6 |
| | B | cluster point, subnet. Filters: Filter, Cofinite filter, neighbourhood filter, filter base | | | CO6 |
| | C | convergent filter and Zorn's lemma | | | CO6 |
| | Mode of examination | Theory | | | |
| | Weightage Distribution | CA | MTE | ETE | |
| | | 30% | 20% | 50% | |
| | Text book/s* | 1. S. Kumaresan, Topology of Metric Spaces, 2nd Ed., Narosa Publishing House, 2011. 2. Dugundji, James, Topology, Allyn and Bacon Series in Advanced Mathematics, Allyn and Bacon, Inc., Boston, Mass.-London-Sydney, 1978. | | | |
| | Other References | 1. Munkres, James R, Topology: A First Course, Prentice-Hall, Inc., Englewood Cliffs, N.J., 1975. 2. Kelley, John L., General Topology, Graduate Texts in Mathematics, No. 27, Springer-Verlag, New York-Berlin, 1975. | | | |

COURSE OUTCOMES – PROGRAMME OUTCOMES MAPPING TABLE

| PO | PO1 | PO2 | PO3 | PO4 | PO5 | PSO1 | PSO2 | PSO3 | PSO4 |
|---------------|----------|----------|----------|----------|----------|----------|----------|----------|----------|
| CO | | | | | | | | | |
| C107.1 | 3 | 3 | 3 | 3 | 2 | 3 | 3 | 2 | 1 |
| C107.2 | 3 | 2 | 3 | 3 | 3 | 3 | 2 | 1 | 2 |
| C107.3 | 2 | 2 | 2 | 3 | 2 | 2 | 2 | 1 | 1 |
| C107.4 | 2 | 2 | 1 | 2 | 2 | 2 | 3 | 1 | 1 |
| C107.5 | 3 | 2 | 2 | 3 | 2 | 3 | 2 | 2 | 2 |
| C107.6 | 3 | 2 | 1 | 3 | 2 | 2 | 2 | 1 | 2 |

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|----------------------------|-----------------------|---|
| School: SBSR | | Batch : 2018-20 |
| Program: M. Sc. | | Current Academic Year: 2018 - 19 |
| Branch: Mathematics | | Semester: II |
| 1 | Course Code | MMT 108 |
| 2 | Course Title | DIFFERENTIAL GEOMETRY & TENSOR ANALYSIS |
| 3 | Credits | 4 |
| 4 | Contact Hours (L-T-P) | 4-0-0 |
| | Course Status | Compulsory |
| 5 | Course Objective | <p>1. Familiarise students with basic concept of local theory of curves: space curves, e.g., plane curves, tangent and normal and binormal; Osculating plane, normal lines and normal plane, curvature and torsion, rectifying plane; Helices, arc length, Serret-Frenet formulae. Have an idea of Bertrand curves and its properties, Contact between curve and surfaces, tangent surfaces, tangent vectors and vector fields, Fundamental theorems for space curves, involutes and evolutes of curves, Metric-first fundamental form and second fundamental form.</p> <p>2. Have an understanding of Normal curvature, quadratic form of normal curvature, mean curvature, Gaussian curvature and minimal surface, geodesics, canonical geodesic equations, normal properties of geodesics, geodesics curvature, lines of curvature, Rodrigue's formula. Know about Tensor calculus, Vector spaces, the dual spaces, tensor product of vector spaces, transformation formulae, contraction, inner product and outer product of two tensor. To know Contra variant and covariant tensors, mixed tensors of higher order, symmetric and skew-symmetric tensors, Quotient theorem, Reciprocal tensors, metric tensor, conjugate metric tensor with examples. Christoffel's symbols, covariant differentiation and Riemannian curvature tensor.</p> |
| 6 | Course | CO1: Describe the concept of local theory of curves: space curves, Osculating plane, |

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| | Outcomes | <p>normal lines and normal plane and explain curvature and torsion rectifying plane; Helices, arc length, Serret-Frenet formulae. (K1,K2,K4)</p> <p>CO2: Explain the theory of curves: Bertrand curves, Contact between curve and surfaces, tangent surfaces, tangent vectors and vector fields and write Fundamental theorems for space curves, involutes and evolutes of curves describe Metric-first fundamental form and second fundamental form. (K2,K4,K6)</p> <p>CO3: Discuss the concept of curvature and evaluate normal curvature, quadratic form of normal curvature, mean curvature, Gaussian curvature and minimal surface, geodesics, canonical geodesic equations, normal properties of geodesics, geodesics curvature, lines of curvature, Rodrigue's formula. (K1,K2,K5)</p> <p>CO4: Explain Tensor calculus, Vector spaces, and the dual spaces, tensor product of vector spaces, transformation formulae, and contraction; evaluate inner product and outer product of two tensor. (K2,K4,K5)</p> <p>CO5: Describe the concept of contra variant and covariant tensors, mixed tensors of higher order, symmetric and skew-symmetric tensors. (K1,K2)</p> <p>CO6: Write the Quotient theorem, Reciprocal tensors, metric tensor, illustrate conjugate metric tensor with examples. Christoffel's symbols, covariant differentiation and Riemannian curvature tensor.(K3,K6)</p> |
| 7 | Course Description | This course is an introduction to differential geometry and tensor analysis. The primary objective of the course is to develop the advance understanding of differential geometry and tensor analysis. |
| 8 | Outline syllabus | CO Mapping |
| | Unit 1 | Review of local theory of curves |
| | A | Space curves, e.g., plane curves, tangent and normal and binormal |
| | B | Osculating plane, normal lines and normal plane, curvature and torsion |
| | C | Rectifying plane; Helices, arc length, Serret-Frenet formulae. |
| | Unit 2 | Theory of Curves |
| | A | Bertrand curves and its properties, Contact between curve and surfaces, tangent surfaces, tangent vectors and vector fields |
| | B | Fundamental theorems for space curves, involutes and evolutes of curves |
| | C | Metric-first fundamental form and second fundamental form. |
| | Unit 3 | Curvature |
| | A | Normal curvature, quadratic form of normal curvature, mean curvature |
| | B | Gaussian curvature and minimal surface, geodesics, canonical geodesic equations |
| | C | Normal properties of geodesics, geodesics curvature, lines of curvature, Rodrigue's formula |
| | Unit 4 | Tensor calculus |
| | A | Tensor calculus, Vector spaces, the dual spaces |

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|--|------------------------|--|-----|-----|-----|
| | B | Tensor product of vector spaces, transformation formulae, contraction | | | CO4 |
| | C | Inner product and outer product of two tensor | | | CO4 |
| | Unit 5 | Contra variant and covariant tensors | | | |
| | A | Contra variant and covariant tensors, mixed tensors of higher order, symmetric and skew-symmetric tensors | | | CO5 |
| | B | Quotient theorem, Reciprocal tensors, metric tensor, conjugate metric tensor with examples | | | CO6 |
| | C | Christoffel's symbols, covariant differentiation and Riemannian curvature tensor. | | | CO6 |
| | Mode of examination | Theory | | | |
| | Weightage Distribution | CA | MTE | ETE | |
| | | 30% | 20% | 50% | |
| | Text book/s* | 1. Elementary Differential Geometry, Revised 2 nd Edition, by Barrett O'Neill 2. Differential Geometry by J.J Stoker, John Wiley and Sons. | | | |
| | Other References | 1. Schaum's Outline Series of Differential Geometry | | | |

COURSE OUTCOMES – PROGRAMME OUTCOMES MAPPING TABLE

| PO | PO1 | PO2 | PO3 | PO4 | PO5 | PSO1 | PSO2 | PSO3 | PSO4 |
|---------------|-----|-----|-----|-----|-----|------|------|------|------|
| CO | | | | | | | | | |
| C108.1 | 3 | 3 | 3 | 3 | 3 | 3 | 3 | 2 | 1 |
| C108.2 | 3 | 2 | 3 | 3 | 2 | 3 | 2 | 1 | 2 |
| C108.3 | 2 | 2 | 3 | 2 | 3 | 2 | 2 | 2 | 1 |
| C108.4 | 2 | 2 | 1 | 2 | 2 | 2 | 3 | 1 | 2 |
| C108.5 | 3 | 2 | 2 | 3 | 2 | 3 | 2 | 2 | 2 |
| C108.6 | 3 | 2 | 1 | 3 | 2 | 2 | 2 | 1 | 2 |

| | | | |
|----------------------------|-----------------------|---|------------|
| School: SBSR | | Batch : 2018-20 | |
| Program: M. Sc. | | Current Academic Year: 2019-20 | |
| Branch: Mathematics | | Semester: III | |
| 1 | Course Code. | MMT-201 | |
| 2 | Course Title | ABSTRACT ALGEBRA | |
| 3 | Credits | 4 | |
| 4 | Contact Hours (L-T-P) | 4-0-0 | |
| | Course status | Compulsory | |
| 5 | Course Objective | 1. To familiarise students with basic concepts of group, subgroup, quotient group and permutation groups, and given an idea of the normal subgroup, sylow groups, internal and external direct product. 2. To make students familiar with the concept of homomorphism, isomorphism, automorphism and inner- automorphism, different algebraic structures ring, integral domain, field, ideal and quotient ring, prime and maximal ideal, Irreducible polynomials, principal ideal domains and unique factorization domains. Know about Extension of fields: algebraic extensions, roots of polynomials and splitting fields. | |
| 6 | Course Outcomes | CO1: Explain and illustrate the concept of group, subgroup, quotient group and permutation groups.(K2,K3,K4) CO2: Describe the normal subgroup, sylow groups and evaluate internal and external direct product. (K1,K2,K5) CO3: Explain the concepts of homomorphism, isomorphism and analysis automorphism and inner- automorphism. (K2,K4) CO4: Discuss about ring integral domain, field ideal and quotient ring, prime and maximal ideal. (K2) CO5: Evaluate irreducible polynomials, principal ideal domains and unique factorization domains. (K5) CO6: Explain about Extension of fields: algebraic extensions and evaluate roots of polynomials and splitting fields. (K2,K4,K5) | |
| 7 | Course Description | This course is an introduction to concept of groups, normal subgroups. The primary objective of the course is to develop the understanding of rings and fields. | |
| 8 | Outline syllabus | | CO Mapping |
| | Unit 1 | Review of Groups | |
| | A | Subgroups, quotient groups, | CO1 |
| | B | Permutation group, | CO1 |
| | C | Lagrange's theorem and the result about its converse. | CO1 |
| | Unit 2 | Normal Subgroups and Sylow theorem | |
| | A | Normal subgroups and factor groups and applications. | CO2 |
| | B | Cauchy's and Sylow's theorems and applications, | CO2 |
| | C | Finitely generated Abelian groups, internal and external direct products. Examples. | CO2 |

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| | | | |
| | Unit 3 | Homomorphism and Isomorphism | |
| | A | Homomorphism of groups, kernel of a homomorphism, | CO3 |
| | B | Definition of isomorphism, Automorphism, | CO3 |
| | C | Inner automorphisms. | CO3 |
| | Unit 4 | Ring Theory | |
| | A | Rings, Integral Domains and Fields: Ideal and quotient Rings, | CO4 |
| | B | Prime and maximal ideals, polynomial rings, irreducible polynomials, | CO4, CO5 |
| | C | Eisenstein criterion, principal ideal domains and unique factorization domains. | CO4, CO5 |
| | Unit 5 | Extension of fields | |
| | A | Algebraic extensions | CO6 |
| | B | Roots of polynomials | CO6 |
| | C | Splitting fields | CO6 |
| | Mode of examination | Theory | |
| | Weightage | CA | MTE |
| | Distribution | 30% | 20% |
| | | ETE | 50% |
| | Text book/s* | 1. Joseph Gallian, contemporary Abstract algebra, seventh edition USA. 2. P. B. Bhattacharya, S. K. Jain and S. R. Nagpal, Basic Abstract Algebra (2nd Edition) Cambridge University Press, Indian Edition, 1977. | |
| | Other References | 1. I. N. Herstein, Topics in Algebra, Wiley Eastern Ltd., New Delhi, 1975. 2. N. Jacobson, Basic Algebra, Vol I & II, W.H. Freeman, 1980 (also published by Hindustan Publishing Company). 3. V. K. Khanna and S. K. Bhamri, A course in abstract Algebra, 3 rd .Ed. 2008. 4. N.S. Gopalakrishnan: University Algebra. | |

COURSE OUTCOMES – PROGRAMME OUTCOMES MAPPING TABLE

| PO | PO1 | PO2 | PO3 | PO4 | PO5 | PSO1 | PSO2 | PSO3 | PSO4 |
|---------------|----------|----------|----------|----------|----------|----------|----------|----------|----------|
| CO | | | | | | | | | |
| C201.1 | 3 | 3 | 3 | 3 | 3 | 3 | 3 | 2 | 1 |
| C201.2 | 3 | 2 | 3 | 3 | 2 | 3 | 2 | 1 | 2 |
| C201.3 | 2 | 2 | 2 | 3 | 3 | 2 | 2 | 1 | 1 |
| C201.4 | 2 | 2 | 2 | 3 | 2 | 2 | 3 | 2 | 2 |
| C201.5 | 3 | 2 | 2 | 3 | 2 | 3 | 2 | 2 | 2 |
| C201.6 | 3 | 2 | 1 | 3 | 2 | 2 | 2 | 1 | 2 |

| | | |
|----------------------------|-----------------------|--|
| School: SBSR | | Batch : 2018-20 |
| Program: M.Sc. | | Current Academic Year: 2019-2020 |
| Branch: Mathematics | | Semester: III |
| 1 | Course Code | MMT 203 |
| 2 | Course Title | LINEAR PROGRAMMING |
| 3 | Credits | 4 |
| 4 | Contact Hours (L-T-P) | 4-0-0 |
| | Course Status | Compulsory |
| 5 | Course Objective | To make students familiar with the concepts of simple analytical Methods to solve L.P.P., queuing theory with kendall's notations, inventory control with ABC analysis, Project Management (CPM & PERT). |
| 6 | Course Outcomes | CO1: Discuss the origins of Operation Research, formulate the problems in L.P. and solve it by graphical. (K1, K3, K6) CO2: Explain analytical Methods: Simplex, Big M, Primal and Dual problems and discuss about economic interpretation of dual. (K2,K3, K4) CO3: Describe queuing theory and Kendall's Notations and formulate |

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| | | M/M/1:∞/FCFS model illustrate with example. (K2, K3, K6) CO4: Explain inventory classifications and develop economic order quantity models. (K2, K4, K6) CO5: Explain ABC analysis. (K2,K4) CO6: Describe the concept of CPM and PERT and calculate float calculation and Cost reduction by Crashing of activities. (K1, K2,K3) | | |
| 7 | Course Description | This course is an introduction to concept of linear programming problems. The primary objective of the course is to develop the understanding of queuing theory with kendall's notations, inventory control with ABC analysis, Project Management (CPM & PERT). | | |
| 8 | Outline syllabus | | | CO Mapping |
| | Unit 1 | Origin of Operation Research | | |
| | A | Origin of Operation Research, Historical Standpoint, Methodology, Different Phases. | | CO1 |
| | B | Characteristics, Scope and Application of Operations Research. Introduction. | | CO1 |
| | C | Requirement of LP, Basic Assumptions, Formulation of LP, General Statement of LP, Solution techniques of LP: Graphical Methods. | | CO1 |
| | Unit 2 | Analytical Methods | | |
| | A | Analytical Methods: Simplex. | | CO2 |
| | B | Big M, Primal and Dual Problems. | | CO2 |
| | C | Economic Interpretation and Dual Simplex Method. | | CO2 |
| | Unit 3 | Queuing Theory | | |
| | A | Basis of Queuing theory, elements of queuing theory. | | CO3 |
| | B | Kendall's Notation, Operating characteristics of a queuing system, Classification of Queuing models. | | CO3 |
| | C | Preliminary examples of M/M/1:∞/FCFS. | | CO3 |
| | Unit 4 | Inventory Control | | |
| | A | Inventory classification, Different cost associated to Inventory. | | CO4 |
| | B | Economic order quantity, Inventory models with deterministic demands | | CO4 |
| | C | ABC analysis. | | CO4, CO5 |
| | Unit 5 | Project Management | | |
| | A | Introduction to PERT and CPM, critical Path calculation. | | CO6 |
| | B | Float calculation and its importance. | | CO6 |
| | C | Cost reduction by Crashing of activity. | | CO6 |
| | Mode of examination | Theory | | |
| | Weightage Distribution | CA | MTE | ETE |
| | | 30% | 20% | 50% |
| | Text book/s* | 1. Taha, H.A., Operations Research-An introduction, New York: MacMillan, 1992. | | |

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|--|---------------------|--|--|
| | | 2. KantiSwarup, P. K. Gupta and Man Mohan: Operation Research ; S. Chand & Sons, New delhi. | |
| | Other References | 1. Hadley, G., Linear Programming, Addison –Wesley, 1962. 2. Hillier, F.S. and G.J. Lieberman, Introduction to Operations Research-concept and cases, Asian Ed., Tata McGraw-Hill. | |

COURSE OUTCOMES – PROGRAMME OUTCOMES MAPPING TABLE

| PO | PO1 | PO2 | PO3 | PO4 | PO5 | PSO1 | PSO2 | PSO3 | PSO4 |
|--------|-----|-----|-----|-----|-----|------|------|------|------|
| CO | | | | | | | | | |
| C203.1 | 3 | 3 | 3 | 3 | 3 | 3 | 3 | 2 | 1 |
| C203.2 | 3 | 2 | 3 | 3 | 2 | 3 | 2 | 1 | 2 |
| C203.3 | 2 | 2 | 2 | 2 | 2 | 1 | 2 | 2 | 1 |
| C203.4 | 2 | 2 | 1 | 3 | 2 | 2 | 3 | 1 | 1 |
| C203.5 | 3 | 1 | 2 | 3 | 2 | 3 | 2 | 2 | 2 |
| C203.6 | 3 | 2 | 1 | 3 | 2 | 2 | 2 | 1 | 1 |

| | | |
|----------------------------|--------------------------|---|
| School: SBSR | | Batch : 2018-20 |
| Program: M.Sc. | | Current Academic Year: 2019-20 |
| Branch: Mathematics | | Semester: III |
| 1 | Course Code | MMT-209 |
| 2 | Course Title | Graph Theory and its Application |
| 3 | Credits | 4 |
| 4 | Contact Hours (L-T-P) | 4-0-0 |
| | Course Status | Compulsory |
| 5 | Course Objective | The goal of this course is to introduce the necessary mathematical concepts of relevant vocabulary from graph theory and combinatory, and know the statements and proofs of many of the important theorems in the subject, and be able to perform related calculations. |
| 6 | Course Outcomes | CO1: Describe the basic concept of graphs and evaluate distances, radius, diameter, centre of a graph, the number of distinct spanning trees in a complete graph. (K2,K4,K5) CO2: Explain the concept of tree and write Kruskal and Prim algorithms, Huffman's algorithm. (K2,K4,K6) CO3: Discuss about matching of graphs and write the theorems |

| | | related to matching. (K1,K2,K6) CO4: Describe graph colouring, chromatic number, bounds on chromatic numbers and write Greedy algorithm. (K2,K6) CO5: Discuss interval graphs and chordal graphs, chromatic polynomials and write Brook's theorem. (K1, K2, K6) CO6: Explain Hamilton property, Non-Hamiltonian graphs, Non-planarity of K_5 and $K_{3,3}$, classification of regular polytopes and write 5-colour theorem. Ramsey theory. (K2,K4,K6) | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
|---------------|---|--|--|---|-------------------|---------------|------------------------|--|---|---|-----|---|---|-----|---|--|-----|---------------|---------------|--|---|---|-----|---|--|-----|---|---|-----|---------------|------------------|--|---|---|-----|---|--|-----|---|---|-----|---------------|--------------------------|--|---|---|-----|---|---|-----|
| 7 | Course Description | This course covers the theory of graphs and networks for both directed and undirected graphs. Topics include graph isomorphism, Eulerian and Hamiltonian graphs, matching, covers, connectivity, coloring, and planarity. There is an emphasis on applications to real world problems and on graph algorithms such as those for spanning trees, shortest paths, and network flows. | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| 8 | Outline syllabus | <table border="1"> <thead> <tr> <th></th><th>Graph Theory and its Application</th><th>CO Mapping</th></tr> </thead> <tbody> <tr> <td>Unit 1</td><td>Basic Concepts.</td><td></td></tr> <tr> <td>A</td><td>Various kinds of graphs, simple graphs, complete graph, walk, tour, path and cycle, Eulerian graph, bipartite graph (characterization).</td><td>CO1</td></tr> <tr> <td>B</td><td>Havel-Hakimi theorem and Erdos-Gallai theorem (statement only), hypercube graph, Petersen graph, trees, forests and spanning subgraphs.</td><td>CO1</td></tr> <tr> <td>C</td><td>Distances, radius, diameter, center of a graph, the number of distinct spanning trees in a complete graph.</td><td>CO1</td></tr> <tr> <td>Unit 2</td><td>Trees:</td><td></td></tr> <tr> <td>A</td><td>Kruskal and Prim algorithms with proofs of correctness, Dijkstra's algorithm,</td><td>CO2</td></tr> <tr> <td>B</td><td>Breadth first and Depth first search trees</td><td>CO2</td></tr> <tr> <td>C</td><td>Rooted and binary trees, Huffman's algorithm.</td><td>CO2</td></tr> <tr> <td>Unit 3</td><td>Matching:</td><td></td></tr> <tr> <td>A</td><td>Augmenting path, Hall's matching theorem, vertex and edge cover, independence number and their connections, Tutte's theorem for the existence of a 1-factor in a graph.</td><td>CO3</td></tr> <tr> <td>B</td><td>Connectivity k-vertex and edge connectivity, blocks, characterizations of 2- connected graphs, Menger's theorem and applications</td><td>CO3</td></tr> <tr> <td>C</td><td>Network flows, Ford- Fulkerson algorithm, Supply-demand theorem and the Gale-Ryser theorem on degree sequences of bipartite graphs.</td><td>CO3</td></tr> <tr> <td>Unit 4</td><td>Graph Colourings:</td><td></td></tr> <tr> <td>A</td><td>chromatic number, Greedy algorithm, bounds on chromatic numbers</td><td>CO4</td></tr> <tr> <td>B</td><td>interval graphs and chordal graphs (with simplicial</td><td>CO5</td></tr> </tbody> </table> | | Graph Theory and its Application | CO Mapping | Unit 1 | Basic Concepts. | | A | Various kinds of graphs, simple graphs, complete graph, walk, tour, path and cycle, Eulerian graph, bipartite graph (characterization). | CO1 | B | Havel-Hakimi theorem and Erdos-Gallai theorem (statement only), hypercube graph, Petersen graph, trees, forests and spanning subgraphs. | CO1 | C | Distances, radius, diameter, center of a graph, the number of distinct spanning trees in a complete graph. | CO1 | Unit 2 | Trees: | | A | Kruskal and Prim algorithms with proofs of correctness, Dijkstra's algorithm, | CO2 | B | Breadth first and Depth first search trees | CO2 | C | Rooted and binary trees, Huffman's algorithm. | CO2 | Unit 3 | Matching: | | A | Augmenting path, Hall's matching theorem, vertex and edge cover, independence number and their connections, Tutte's theorem for the existence of a 1-factor in a graph. | CO3 | B | Connectivity k-vertex and edge connectivity, blocks, characterizations of 2- connected graphs, Menger's theorem and applications | CO3 | C | Network flows, Ford- Fulkerson algorithm, Supply-demand theorem and the Gale-Ryser theorem on degree sequences of bipartite graphs. | CO3 | Unit 4 | Graph Colourings: | | A | chromatic number, Greedy algorithm, bounds on chromatic numbers | CO4 | B | interval graphs and chordal graphs (with simplicial | CO5 |
| | Graph Theory and its Application | CO Mapping | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| Unit 1 | Basic Concepts. | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| A | Various kinds of graphs, simple graphs, complete graph, walk, tour, path and cycle, Eulerian graph, bipartite graph (characterization). | CO1 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| B | Havel-Hakimi theorem and Erdos-Gallai theorem (statement only), hypercube graph, Petersen graph, trees, forests and spanning subgraphs. | CO1 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| C | Distances, radius, diameter, center of a graph, the number of distinct spanning trees in a complete graph. | CO1 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| Unit 2 | Trees: | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| A | Kruskal and Prim algorithms with proofs of correctness, Dijkstra's algorithm, | CO2 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| B | Breadth first and Depth first search trees | CO2 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| C | Rooted and binary trees, Huffman's algorithm. | CO2 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| Unit 3 | Matching: | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| A | Augmenting path, Hall's matching theorem, vertex and edge cover, independence number and their connections, Tutte's theorem for the existence of a 1-factor in a graph. | CO3 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| B | Connectivity k-vertex and edge connectivity, blocks, characterizations of 2- connected graphs, Menger's theorem and applications | CO3 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| C | Network flows, Ford- Fulkerson algorithm, Supply-demand theorem and the Gale-Ryser theorem on degree sequences of bipartite graphs. | CO3 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| Unit 4 | Graph Colourings: | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| A | chromatic number, Greedy algorithm, bounds on chromatic numbers | CO4 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| B | interval graphs and chordal graphs (with simplicial | CO5 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |

Beyond Boundaries

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|--|------------------------|--|-----|-----|-----|
| | | elimination ordering), | | | |
| | C | Brook's theorem and graphs with no triangles but large chromatic number, chromatic polynomials. | | | CO5 |
| | Unit 5 | Hamilton property: | | | |
| | A | Necessary conditions, Theorems of Dirac and Ore, Chvatal's theorem and toughness of a graph. | | | CO6 |
| | B | Non-Hamiltonian graphs with large vertex degrees. Planar graphs Embedding a graph on plane, Euler's formula. | | | CO6 |
| | C | Non-planarity of K5 and K3,3, classification of regular polytopes, Kuratowski's theorem (no proof), 5-colour theorem. Ramsey theory. | | | CO6 |
| | Mode of examination | Theory | | | |
| | Weightage Distribution | CA | MTE | ETE | |
| | | 30% | 20% | 50% | |
| | Text book | 1. B. West, Introduction to Graph Theory, Prentice Hall of India, 2001. | | | |
| | Other References | 1. J. A. Bondy and U. S. R. Murty, Graph Theory with Applications, Springer-Verlag, 2008. 2. R. Diestel, Introduction to Graph Theory, Springer-Verlag, 2010. | | | |

COURSE OUTCOMES – PROGRAMME OUTCOMES MAPPING TABLE

| PO | PO1 | PO2 | PO3 | PO4 | PO5 | PSO1 | PSO2 | PSO3 | PSO4 |
|--------|-----|-----|-----|-----|-----|------|------|------|------|
| CO | | | | | | | | | |
| C209.1 | 3 | 3 | 3 | 3 | 3 | 3 | 3 | 2 | 1 |
| C209.2 | 3 | 2 | 3 | 3 | 2 | 3 | 2 | 1 | 2 |
| C209.3 | 2 | 2 | 3 | 2 | 3 | 2 | 2 | 1 | 2 |
| C209.4 | 2 | 3 | 2 | 2 | 2 | 2 | 3 | 3 | 2 |
| C209.5 | 3 | 2 | 2 | 3 | 2 | 3 | 2 | 2 | 2 |
| C209.6 | 3 | 2 | 2 | 3 | 2 | 2 | 2 | 2 | 2 |

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|----------------------------|--------------------------|--|
| School: SBSR | | Batch : 2018-20 |
| Program: M.Sc. | | Current Academic Year: 2019-20 |
| Branch: Mathematics | | Semester: III |
| 1 | Course Code | MMT-204 |
| 2 | Course Title | FLUID DYNAMICS |
| 3 | Credits | 4 |
| 4 | Contact Hours (L-T-P) | 4-0-0 |
| | Course Status | Compulsory |
| 5 | Course Objective | The goal of this course is to introduce the necessary mathematical concepts for analysing fluid dynamics. Learn to perform integral analyses and overall balances from conservation laws and differential equations analyses for fields. Understand modelling approximations such as inviscid, incompressible, and turbulent for different types of flows. |
| 6 | Course Outcomes | CO1: Explain the definition, properties and classification of fluid; define Pascal's law and write basic hydrostatic equation, Buoyancy and Archimedes' principle. (K1, K2,K4,K6) CO2: Describe the streamlines, path lines and streak lines, steady/unsteady, uniform/non-uniform, one-two dimensional flows and evaluate velocity and acceleration in an Eulerian flow field. (K1,K2,K5) CO3: Explain equations for stream function, velocity potential function in rectangular and cylindrical co-ordinates and discuss the concept of equations for source, sink, irrotational vortex, circulation.(K1,K2,K4) CO4: Explain and apply Integral equations for the control volume: using Reynold's Transport theorem. (K2,K3,K4) CO5: Explain equations for conservation of mass, energy and momentum and write Bernoulli's equation and its application. (K2,K4,K6) CO6: Apply Mass conservation in 2 dimension in rectangular co-ordinates, Euler's equations in 2,3 dimensions and subsequent derivation of Bernoulli's equation and write Navier-Stokes equations.(K3,K4,K6) |
| 7 | Course Description | This course is an introduction to basics concept of velocity field, fluid statics, basic conservation laws for systems and control volumes, dimensional analysis and similitude, Euler and Bernoulli equations, NavierStokes equations, viscous flows, boundary-layer flow in channels and around submerged bodies, applications. |
| 8 | Outline syllabus | FLUID DYNAMICS CO Mapping |

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|--|------------------------|--|-----|-----|-----|
| | Unit 1 | | | | |
| | A | Fluid Definition and properties, Newton's law of viscosity concept of continuum, Classification of fluids. | | | CO1 |
| | B | Definition of body and surface forces, Pascal's law, Basic hydrostatic equation, | | | CO1 |
| | C | Forces on surfaces due to hydrostatic pressure, Buoyancy and Archimedes' principle. | | | CO1 |
| | Unit 2 | | | | |
| | A | Eulerian and Lagrangian approach to solutions; Velocity and acceleration in an Eulerian flow field; | | | CO2 |
| | B | Definition of streamlines, path lines and streak lines; Definition of steady/unsteady, uniform/non-uniform, one-two dimensional flows; | | | CO2 |
| | C | Definition of control volume and control surface, Understanding of differential and integral methods of analysis | | | CO2 |
| | Unit 3 | | | | |
| | A | Definition and equations for stream function, velocity potential function in rectangular and cylindrical co-ordinates | | | CO3 |
| | B | Rotational and irrotational flows; | | | CO3 |
| | C | Definition and equations for source, sink, irrotational vortex, circulation. | | | CO3 |
| | Unit 4 | | | | |
| | A | Integral equations for the control volume: Reynold's Transport theorem (without proof), | | | CO4 |
| | B | Equations for conservation of mass, energy and momentum, | | | CO5 |
| | C | Bernoulli's equation and its application | | | CO5 |
| | Unit 5 | | | | |
| | A | Differential equations for the control volume: Mass conservation in 2 dimension in rectangular co-ordinates, | | | CO6 |
| | B | Euler's equations in 2,3 dimensions and subsequent derivation of Bernoulli's equation; | | | CO6 |
| | C | Navier-Stokes equations (without proof) in rectangular Cartesian co-ordinates | | | CO6 |
| | Mode of examination | Theory | | | |
| | Weightage Distribution | CA | MTE | ETE | |
| | | 30% | 20% | 50% | |
| | Text book | 1. Fluid Mechanics : Streeter and Wylie, McGraw Hill | | | |
| | Other References | 1. Fluid Mechanics : F.M.White, McGraw Hill | | | |

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| | | 2. Fluid Dynamics, M. D. Raisinghania, S Chand Group | |
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COURSE OUTCOMES – PROGRAMME OUTCOMES MAPPING TABLE

| PO | PO1 | PO2 | PO3 | PO4 | PO5 | PSO1 | PSO2 | PSO3 | PSO4 |
|--------|-----|-----|-----|-----|-----|------|------|------|------|
| CO | | | | | | | | | |
| C204.1 | 3 | 3 | 3 | 3 | 3 | 3 | 3 | 2 | 1 |
| C204.2 | 3 | 2 | 3 | 3 | 2 | 3 | 2 | 1 | 2 |
| C204.3 | 2 | 3 | 2 | 2 | 3 | 2 | 2 | 1 | 2 |
| C204.4 | 2 | 2 | 1 | 3 | 2 | 2 | 3 | 2 | 1 |
| C204.5 | 3 | 2 | 2 | 3 | 2 | 3 | 2 | 2 | 2 |
| C204.6 | 3 | 2 | 2 | 3 | 2 | 2 | 2 | 2 | 2 |

| | | |
|----------------------------|-----------------------|---|
| School: SBSR | | Batch : 2018-20 |
| Program: M.Sc. | | Current Academic Year: 2019-20 |
| Branch: Mathematics | | Semester: III |
| 1 | Course Code | MMT 206 |
| 2 | Course Title | Number Theory with Cryptography |
| 3 | Credits | 4 |
| 4 | Contact Hours (L-T-P) | 4-0-0 |
| | Course Status | Compulsory |
| 5 | Course Objective | To make students familiar with the basic concepts of number theory, congruence. Also students are able to understand public & private key cryptography. |

| | | | |
|---|---|---|------------|
| 6 | Course Outcomes | <p>CO1: Explain the basic concepts of number theory and calculate GCD, LCM; write factorization theorem, Euclid theorem, and Prime number theorem. (K2,K3,K4,K6)</p> <p>CO2: Discuss about congruences along with solutions, residue system, write Fermat's little theorem, Wilson theorem, Chinese remainder theorem, Hansel lemma and calculate Primitive roots. (K1,K2,K5,K6)</p> <p>CO3: Describe classical encryption techniques, Substitution ciphers and transposition ciphers, modern block ciphers principles, public & private key cryptography, write RSA algorithm. (K2,K6)</p> <p>CO4: Discuss and write Gauss lemma, Legendre symbol, quadratic reciprocity law, Jacobi symbol.(K2,K6)</p> <p>CO5: Explain the greatest integer function, Euler's totient function, the number of divisors function.(K2,K4)</p> <p>CO6: Discuss and evaluate the sum of divisors function, Mobius mu function, Mobius inversion formula. (K1,K2,K5)</p> | |
| 7 | Course Description | This course is an introduction to basics of number theory with cryptography, congruences, quadratic residues, some standard arithmetic functions. | |
| 8 | Outline syllabus : Number theory with Cryptography (MMT-206) | | CO Mapping |
| | Unit 1 | BASICS | |
| | A | Primes, Divisibility, Euclid's algorithm, GCD, LCM, expressing. | CO1 |
| | B | GCD as a linear combination of the numbers, Unique factorization theorem, Euclid's theorem on infinitude of primes. | CO1 |
| | C | Idea of existence of large gaps between primes, Statement of prime number theorem. | CO1 |
| | Unit 2 | CONGRUENCES | |
| | A | Definition, Residue system modulo m, Fermat's little theorem, Euler's generalization of Fermat's theorem. | CO2 |
| | B | Wilson's theorem, Solution of congruences, Chinese remainder theorem. | CO2 |
| | C | Hansel's lemma, Prime power moduli, Primitive roots. | CO2 |
| | Unit 3 | CRYPTOGRAPHY | |
| | A | Classical encryption techniques, Substitution ciphers and transposition ciphers, Modern block ciphers and Block ciphers principles. | CO3 |

| | | | | | |
|--|------------------------|---|-----|-----|-----|
| | B | Public key Cryptography: Public keys , Encrypting the message. | | | CO3 |
| | C | Private keys, decrypting and retrieval of the original message (RSA algorithm). | | | CO3 |
| | Unit 4 | QUADRATIC RESIDUES | | | |
| | A | Gauss lemma. | | | CO4 |
| | B | Legendre symbol, Jacobi symbol. | | | CO4 |
| | C | Quadratic reciprocity law. | | | CO4 |
| | Unit 5 | SOME STANDARD ARITHMETIC FUNCTIONS | | | |
| | A | The greatest integer function, Euler's totient function. | | | CO5 |
| | B | The number of divisors function, The sum of divisors function. | | | CO6 |
| | C | Mobius mu function, Mobius inversion formula. | | | CO6 |
| | Mode of examination | Theory | | | |
| | Weightage Distribution | CA | MTE | ETE | |
| | | 30% | 20% | 50% | |
| | Text book/s* | <ul style="list-style-type: none"> Ivan Niven , Herbert S. Zuckerman , Hugh L. Montgomery: An Introduction to the theory of numbers , John Wiley and Sons (Asia) Pvt. Ltd. G. H. Hardy & E. M. Wright : An Introduction to the theory of Numbers. | | | |
| | Other References | | | | |

COURSE OUTCOMES – PROGRAMME OUTCOMES MAPPING TABLE

| PO | PO1 | PO2 | PO3 | PO4 | PO5 | PSO1 | PSO2 | PSO3 | PSO4 |
|---------------|----------|----------|----------|----------|----------|----------|----------|----------|----------|
| CO | | | | | | | | | |
| C206.1 | 3 | 3 | 3 | 3 | 3 | 3 | 3 | 2 | 1 |
| C206.2 | 3 | 2 | 3 | 3 | 2 | 3 | 2 | 1 | 1 |
| C206.3 | 2 | 2 | 2 | 2 | 2 | 2 | 2 | 1 | 2 |
| C206.4 | 2 | 2 | 1 | 2 | 2 | 2 | 3 | 1 | 1 |
| C206.5 | 3 | 2 | 2 | 3 | 3 | 3 | 2 | 2 | 2 |
| C206.6 | 3 | 2 | 1 | 3 | 2 | 2 | 2 | 1 | 2 |

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|----------------------------|-----------------------|---|
| School: SBSR | | Batch : 2018-20 |
| Program: M.Sc. | | Current Academic Year: 2019-20 |
| Branch: Mathematics | | Semester: IV |
| 1 | Course Code | MMT 205 |
| 2 | Course Title | FUNCTIONAL ANALYSIS |
| 3 | Credits | 4 |
| 4 | Contact Hours (L-T-P) | 4-0-0 |
| | Course Status | Compulsory |
| 5 | Course Objective | To familiarise students with basic concepts of Functional analysis and given an idea of implemented the concepts of Elementary understanding of Normed linear spaces. Can perform basic Bounded linear operator and Know how to calculate system of Inner product spaces. Understand the basic concept of functional analysis and learn basic definitions and terminology associated with to functional analysis. |
| 6 | Course Outcomes | CO1: Describe the basics of functional analysis, normed linear spaces, Holder's inequality, Minkowski's inequality and explain l^p -spaces, equivalence of norms and calculate banach spaces. (K2, K3, K4) CO2: Explain bounded linear spaces, finite dimensional normed space and compactness and evaluate dual of normed spaces \mathbb{R}^n ; l^p also of $C[a, b]$. (K2,K4,K5) CO3: Discuss the concept of open mapping and closed graph theorems, explain uniform boundedness principle and its applications.(K1,K2,K4) CO4: Write Hahn-Banach theorem and its consequence. (K6) CO5: Illustrate Inner product spaces, Hilbert spaces with examples and |

| | | | | |
|---|------------------------|--|-----|------------|
| | | write Projection theorem, Bessel's inequality, existence of complete orthonormal basis of a Hilbert space Riesz representation theorem. (K3,K6) CO6: Describe the concept of bounded linear functional, Hilbert adjoint operator, self adjoint operator, Compact operators and write Riesz-Schauder theorem. (K1,K2,K6) | | |
| 7 | Course Description | The primary objective of the course is to develop the understanding the normed linear spaces, bounded linear operator, open mapping and closed graph theorems and Inner product spaces. | | |
| 8 | Outline syllabus | Foundation course in Mathematics | | CO Mapping |
| | Unit 1 | Normed linear spaces | | |
| | A | Normed linear spaces, Holder's inequality, Minkowski's inequality | | CO1 |
| | B | l^p -spaces, equivalence of norms, equivalence of norms on a finite dimensional space, Riesz lemma, | | CO1 |
| | C | Banach spaces, examples | | CO1 |
| | Unit 2 | Bounded linear operator | | |
| | A | Bounded linear operator, spaces of bounded linear operator | | CO2 |
| | B | Finite dimensional normed space and compactness | | CO2 |
| | C | Dual of normed spaces \mathbb{R}^n ; l^p also of $C[a, b]$. | | CO2 |
| | Unit 3 | Open mapping | | |
| | A | Open mapping and closed graph theorems | | CO3 |
| | B | Uniform boundedness principle and its applications | | CO3 |
| | C | Hahn-Banach theorem and its consequence. | | CO3, CO4 |
| | Unit 4 | Inner product spaces | | |
| | A | Inner product spaces, Hilbert spaces and examples | | CO5 |
| | B | Projection theorem, Bessel's inequality, existence of complete orthonormal basis of a Hilbert space | | CO5 |
| | C | Riesz representation theorem | | CO5 |
| | Unit 5 | Bounded linear functional | | |
| | A | Bounded linear functional. | | CO6 |
| | B | Hilbert adjoint operator, self adjoint operator, Compact operators | | CO6 |
| | C | Riesz-Schauder theorem, self-adjoint compact operators. | | CO6 |
| | Mode of examination | Theory | | |
| | Weightage Distribution | CA | MTE | ETE |
| | | 30% | 20% | 50% |
| | Text book/s* | [1] Kreyszig, Erwin, Introductory Functional Analysis with Applications, Wiley Classics Library, John Wiley & Sons, Inc., New York, 1989. [2] Limaye, Balmohan V., Functional Analysis, second edition, New Age International Publishers Limited, | | |

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| Other References | |
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COURSE OUTCOMES – PROGRAMME OUTCOMES MAPPING TABLE

| PO | PO1 | PO2 | PO3 | PO4 | PO5 | PSO1 | PSO2 | PSO3 | PSO4 |
|--------|-----|-----|-----|-----|-----|------|------|------|------|
| CO | | | | | | | | | |
| C205.1 | 3 | 3 | 3 | 3 | 3 | 3 | 3 | 2 | 2 |
| C205.2 | 3 | 2 | 3 | 3 | 2 | 3 | 3 | 1 | 1 |
| C205.3 | 2 | 2 | 2 | 2 | 2 | 2 | 2 | 2 | 2 |
| C205.4 | 2 | 2 | 1 | 2 | 3 | 2 | 3 | 1 | 1 |
| C205.5 | 3 | 2 | 2 | 3 | 2 | 3 | 2 | 2 | 2 |
| C205.6 | 3 | 2 | 1 | 3 | 2 | 2 | 2 | 1 | 2 |

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|----------------------------|-----------------------|---|
| School: SBSR | | Batch : 2018-20 |
| Program: B.SC | | Current Academic Year: 2019-2020 |
| Branch: Mathematics | | Semester: IV |
| 1 | Course Code | MMT 202 |
| 2 | Course Title | MEASURE THEORY |
| 3 | Credits | 4 |
| 4 | Contact Hours (L-T-P) | 4-0-0 |
| | Course Status | Compulsory |
| 5 | Course Objective | This course provides an introduction to topics involving concepts of Topological space, σ -algebra of measurable sets, Borel sets, measurable functions, Lebesgue measure, integration of complex functions and linear functional. |
| 6 | Course Outcomes | CO1: Explain the concept of Topological spaces and calculate interior, exterior limit point and boundary points. (K2, K3, K4) CO2: Describe the concept of approximation of measurable functions, explain Lebesgue's monotone convergence theorem and Fatou's lemma and evaluate integration of positive functions, term by term differentiation of a series of positive measurable functions. (K1,K2, K5) CO3: Discuss the integration of complex function.(K1, K2) CO4: Explain Lebesgue's dominated convergence theorem, role of sets of measure zero, write extension of a measure to a complete measure. (K2,K4,K6) |

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| | | CO5: Explain integration as linear functional, Topological ingredients and write positive Borel measure, Hausdorff spaces. (K2, K3, K4, K6) CO6: Describe the concept locally compact Hausdorff spaces, support of a complex function, vector space of continuous complex functions with compact support and write Urysohn's lemma, Riesz representation theorem. (K1,K2, K6) | | | |
| 7 | Course Description | This course provides an introduction to topics involving concepts of Topological space and separate axioms, σ -algebra of measurable sets, Borel sets, measurable functions, Lebesgue measure, integration of complex functions and linear functional. The primary objective of the course is to develop the advance understanding of Measure Theory. | | | |
| 8 | Outline syllabus | | | CO Mapping | |
| | Unit 1 | Preliminaries: | | | |
| | A | Topological spaces, continuous functions | | CO1 | |
| | B | σ -algebra of measurable sets, Borel sets, measurable functions | | CO1 | |
| | C | lim sup and liminf of sequence of functions. | | CO1 | |
| | Unit 2 | Lebesgue measure: | | | |
| | A | Approximation of measurable functions by simple functions, positive measures | | CO2 | |
| | B | Integration of positive functions, Lebesgue's monotone convergence theorem | | CO2 | |
| | C | Term by term differentiation of a series of positive measurable functions, Fatou's lemma. | | CO2 | |
| | Unit 3 | Integration of complex functions: | | | |
| | A | Complex measurable functions, integration of Complex measurable functions | | CO3 | |
| | B | Lebesgue's dominated convergence theorem , role of sets of measure zero | | CO3, CO4 | |
| | C | Extension of a measure to a complete measure. | | CO3, CO4 | |
| | Unit 4 | Integration as a linear functional: | | | |
| | A | Positive Borel measure, vector spaces | | CO5 | |
| | B | Integration as a linear functional, Topological ingredients | | CO5 | |
| | C | Definition of compactness and Hausdorff spaces. | | CO5 | |
| | Unit 5 | Riesz representation theorem: | | | |
| | A | Locally compact Hausdorff spaces, support of a complex function | | CO6 | |
| | B | Vector space of continuous complex functions with compact support | | CO6 | |
| | C | Urysohn's lemma, Riesz representation theorem. | | CO6 | |
| | Mode of examination | Theory | | | |
| | Weightage Distribution | CA 30% | MTE 20% | ETE 50% | |
| | Text book/s* | 1) Walter Rudin: Real and Complex analysis, Mc | | | |

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| | | GRAW HILL, International student edition. | |
| | Other References | 1) Walter Rudin: Real and Complex analysis, Mc GRAW HILL, International student edition. 2) Walter Rudin: Principles of Mathematical analysis, Mc GRAW HILL, International series in Pure and Applies Mathematics. H. L. Royden: Real Analysis, Amazon. Com. | |

COURSE OUTCOMES – PROGRAMME OUTCOMES MAPPING TABLE

| PO | PO1 | PO2 | PO3 | PO4 | PO5 | PSO1 | PSO2 | PSO3 | PSO4 |
|--------|-----|-----|-----|-----|-----|------|------|------|------|
| CO | | | | | | | | | |
| C202.1 | 3 | 3 | 3 | 3 | 3 | 3 | 3 | 2 | 1 |
| C202.2 | 3 | 2 | 3 | 3 | 2 | 3 | 2 | 1 | 1 |
| C202.3 | 2 | 2 | 2 | 2 | 2 | 2 | 2 | 1 | 1 |
| C202.4 | 2 | 2 | 1 | 2 | 2 | 2 | 3 | 1 | 1 |
| C202.5 | 3 | 2 | 2 | 3 | 3 | 3 | 2 | 2 | 2 |
| C202.6 | 3 | 2 | 1 | 3 | 2 | 3 | 2 | 2 | 2 |

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| School: SBSR | | Batch : 2018-20 |
| Program: M.Sc. | | Current Academic Year: 2019-2020 |
| Branch: Mathematics | | Semester: IV |
| 1 | Course Code | MMT-208 |
| 2 | Course Title | DISCRETE MATHEMATICS |
| 3 | Credits | 4 |
| 4 | Contact Hours (L-T-P) | 4-0-0 |
| | Course Status | Compulsory |
| 5 | Course Objective | This course is aimed to provide an advance understanding to the sets and propositions, relations and functions, permutation and combination, graphs, groups and rings. |
| 6 | Course Outcomes | CO1: Discuss the concept of sets, un-countably infinite sets, principle of inclusion and exclusion, multisets, propositions, conditional propositions and evaluate normal forms, Mathematical induction.(K2,K3, K4,K5) CO2: Describe the concept functions, composition of function, invertible functions, discrete properties of binary relations and check the closure of relations. (K3, K6) |

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| | | <p>CO 3: Explain the concept of POSET and lattices, Warshall's algorithm, Equivalence relations and partitions and evaluate Chains, and Anti-chains. Generating Functions, Recurrence relations and discuss linear recurrence relations with constant coefficient, homogeneous solution, total solutions, solutions by method of Generating function. (K2, K4,K5)</p> <p>CO 4: Illustrate the concept permutations and combinations: rule of sum and product, write the algorithms for generation of permutations and combination. (K3, K5,K6)</p> <p>CO 5: Discuss the concept graph, sub-graph, Walks, Path and circuits, Connected graphs, Disconnected graphs and component, evaluate the fundamental circuits, distance, diameters, radius and pendant vertices, rooted and binary trees (K1,K2,K5,K6)</p> <p>CO6: Demonstrate the understanding of Algebraic systems, Group and evaluate Semi-groups, Monoid, Subgroups, Isomorphism and Automorphism. (K2, K5)</p> |
| 7 | Course Description | This course is given the deep knowledge of sets and propositions, relations and functions, permutation and combination, graphs, groups and rings. |
| 8 | Outline syllabus | CO Mapping |
| | Unit 1 | Sets and Propositions: |
| | A | Sets, Un-countably infinite sets, Principle of inclusion and exclusion, multisets, propositions, conditional propositions. |
| | B | Logical connectivity, Propositional, calculus, Universal and existential quantifiers |
| | C | Normal forms, methods of proofs, Mathematical induction. |
| | Unit 2 | Relations and Functions: |
| | A | Functions , Composition of function , invertible functions, Discrete properties of binary relations, closure of relations |
| | B | Warshall's algorithm, Equivalence relations and partitions, POSET and lattices, Chains, and Anti-chains. Generating Functions, Recurrence relations |
| | C | Linear Recurrence relations with constant coefficient, Homogeneous solution, Total Solutions, Solutions by method of Generating function. |
| | Unit 3 | Permutation and Combination: |
| | A | Permutations and combinations : Rule of sum and Product |
| | B | Permutations, Combination |
| | C | Algorithms for Generation of Permutations and Combination. |
| | Unit 4 | Graphs: |
| | A | Graph, Sub-graph, Various examples of graph and |

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| | | their subgraphs, Walks, Path and circuits, Connected graphs, Disconnected graphs and component | |
| B | | Euler's graphs, various operation on graphs, Hamiltonian Paths and circuits. Trees and fundamental circuits, distance, diameters, radius and pendant vertices, rooted and binary trees | CO5 |
| C | | Counting tree, Spanning tree, Fundamental circuits, Finding all spanning trees, Fundamental circuits. | CO5 |
| Unit 5 | | Groups and Rings: | |
| A | | Algebraic systems, Group | CO6 |
| B | | Semi-groups, Monoid, Subgroups | CO6 |
| C | | Isomorphism and Automorphism. | CO6 |
| Mode of examination | | Theory | |
| Weightage Distribution | CA | MTE | ETE |
| | 30% | 20% | 50% |
| Text book/s* | 1. Liu C.L. and Mohapatra, D.P., "Elements of Discrete Mathematics", SiE edition, TMH, 2008 | | |
| Other References | 1) Kenneth H.R., 'Discrete Mathematics and its Applications', Mc-graw hill. 2) Biggs N., "Discrete Mathematics", 3rd edition, Oxford University | | |

COURSE OUTCOMES – PROGRAMME OUTCOMES MAPPING TABLE

| PO | PO1 | PO2 | PO3 | PO4 | PO5 | PSO1 | PSO2 | PSO3 | PSO4 |
|--------|-----|-----|-----|-----|-----|------|------|------|------|
| CO | | | | | | | | | |
| C208.1 | 3 | 3 | 3 | 3 | 3 | 3 | 3 | 2 | 1 |
| C208.2 | 3 | 2 | 3 | 3 | 2 | 3 | 2 | 1 | 2 |
| C208.3 | 2 | 3 | 2 | 3 | 2 | 2 | 2 | 2 | 1 |
| C208.4 | 2 | 2 | 1 | 2 | 2 | 2 | 3 | 2 | 2 |
| C208.5 | 3 | 2 | 2 | 3 | 2 | 3 | 2 | 2 | 2 |
| C208.6 | 3 | 2 | 2 | 3 | 2 | 2 | 2 | 1 | 2 |

Syllabus of MMT-151 (Practical)

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|----------------------------|-----------------------|--|
| School: SBSR | | Batch : 2018-20 |
| Program: M.Sc. | | Current Academic Year: 2018-19 |
| Branch: Mathematics | | Semester: I |
| 1 | Course Code | MMT-151 |
| 2 | Course Title | Mathematics Lab I |
| 3 | Credits | 2 |
| 4 | Contact Hours (L-T-P) | 0-0-3 |
| | Course Status | Compulsory |
| 5 | Course Objective | The goal of this course is to introduce students to the fundamental mathematical concepts for MATLAB. The course will cover the syntax and semantics of MATLAB including control structures, comments, variables, functions etc. Once the foundations of the language have been established students will explore different types of scientific programming problems including curve fitting, ODE solving etc |
| 6 | Course Outcomes | CO1: Describe the fundamentals of MATLAB and use MATLAB for interactive computations. (K2, K3) CO2: Demonstrate with strings and matrices and their uses. (K2, K3) CO3: Illustrate basic flow controls (if-else, for, while). (K3) CO4: Create plots and export this for use in reports and presentations. (K3, K5) CO5: Develop program scripts and functions using the MATLAB development environment. (K4, K5) |
| 7 | Course Description | The course will give the fundamental knowledge and practical abilities in MATLAB required to effectively utilize this tool in technical numerical computations and visualisation in other courses. Syntax and interactive computations, programming in MATLAB using scripts and functions, rudimentary algebra and analysis. One- and two-dimensional graphical presentations. Examples on engineering applications. |
| 8 | Outline syllabus | CO Mapping |
| | Unit 1 | Practical based MATLAB as a calculator. CO1 |
| | | Creating an Array in MATLAB CO1 |
| | Unit 2 | Practical related to -- Mathematical Operations with Arrays CO3 |
| | Unit 3 | Practical related to--- How to make scripts files in MATLAB and do some examples. CO5 |
| | Unit 4 | Practical related to--- Make some function files in MATLAB. Basic two-dimensional and three-dimensional plotting, change in axes and annotation in a figure. CO4,CO5 |

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| | | | |
| | Unit 5 | Practical related to--- If-End statement, If-Else-End statement, nested If-Else-End statement Solving a system of linear equations, curve fitting with polynomials using inbuilt functions such as polyfit. | CO2,CO5 |
| | Mode of examination | Practical & Viva | |
| | Weightage Distribution | CA | MTE |
| | | 60% | 0% |
| | Text book | ETE | |
| | | 40% | |
| | Text book | 1. An introduction to MATLAB : Amos Gilat | |
| | Other References | 1. Applied Numerical Methods with Matlab for engineering and Scientists by stevenchapra, Mcgraw Hill. 2. Getting started with Matlab: RudraPratap | |

COURSE OUTCOMES – PROGRAMME OUTCOMES MAPPING TABLE

| PO CO | PO1 | PO2 | PO3 | PO4 | PO5 | PSO1 | PSO2 | PSO3 | PSO4 |
|----------|-----|-----|-----|-----|-----|------|------|------|------|
| C151.1 | 3 | 3 | 2 | 2 | 2 | 3 | 2 | 2 | 3 |
| C151.2 | 2 | 3 | 3 | 3 | 3 | 2 | 3 | 3 | 2 |
| C151.3 | 2 | 3 | 2 | 2 | 3 | 3 | 3 | 3 | 3 |
| C151.4 | 2 | 3 | 2 | 3 | 2 | 2 | 2 | 3 | 2 |
| C151.5 | 3 | 3 | 2 | 3 | 2 | 2 | 3 | 2 | 3 |

Syllabus of MMT-152 (Practical)

| | | | |
|----------------------------|-----------------------|---|------------|
| School: SBSR | | Batch : 2018-20 | |
| Program: M.Sc. | | Current Academic Year: 2018-19 | |
| Branch: Mathematics | | Semester: II | |
| 1 | Course Code | MSM 152 | |
| 2 | Course Title | Mathematics Lab II | |
| 3 | Credits | 2 | |
| 4 | Contact Hours (L-T-P) | 0-0-3 | |
| | Course Status | Compulsory | |
| 5 | Course Objective | <ul style="list-style-type: none"> To familiarize the student in introducing and exploring MATLAB software. To enable the student on how to approach for solving problems using MATLAB tools. To prepare the students to use MATLAB in their project works. To provide a foundation in use of this software for real time applications. | |
| 6 | Course Outcomes | CO1: Understand the procedures, algorithms, and concepts require to solve specific problems. (K2) CO2: Discuss and develop the algorithms to solve system of linear equations and measure the accuracy. (K2, K5, K6) CO3: Discuss and develop the algorithms to solve finite differences and interpolation and measure the accuracy. (K2, K5, K6) CO4: Discuss and develop the algorithms to solve system of transcendental equations and measure the accuracy. (K2, K5, K6) CO5: Discuss and develop the algorithms to solve divided differences and measure the accuracy. (K2, K5, K6) CO6: Discuss and develop the algorithms to solve numerical differentiation and integration and measure the accuracy. (K2, K5, K6) | |
| 7 | Course Description | This course teaches computer programming to those with little to no previous experience. It uses the programming system and language called MATLAB to do so because it is easy to learn, versatile and very useful for engineers and other professionals. MATLAB is a special-purpose language that is an excellent choice for writing moderate-size programs that solve problems involving the manipulation of numbers. | |
| 8 | Outline syllabus | | CO Mapping |
| | Unit 1 | Lab. Experiment 1: | |
| | | Solution of system of linear equations: | CO1, CO2 |
| | Unit 2 | Lab. Experiment 2: | |
| | | System of Transcendental equations | CO1, CO3 |
| | Unit 3 | Lab. Experiment 3: | |

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|--|---------------------|---|-----|-----|----------|
| | | Finite differences and interpolation: | | | CO1, CO4 |
| | Unit 4 | Lab. Experiment 4: | | | |
| | | Divided differences: | | | CO1,CO5 |
| | Unit 5 | Lab. Experiment 5: | | | |
| | | Numerical differentiation and integration | | | CO1, CO6 |
| | Mode of examination | Practical | | | |
| | Weightage | CA | MTE | ETE | |
| | Distribution | 60% | 0% | 40% | |
| | Text book/s* | Amos Gilot | | | |
| | Other References | | | | |

COURSE OUTCOMES – PROGRAMME OUTCOMES MAPPING TABLE

| PO | PO1 | PO2 | PO3 | PO4 | PO5 | PSO1 | PSO2 | PSO3 | PSO4 |
|--------|-----|-----|-----|-----|-----|------|------|------|------|
| CO | | | | | | | | | |
| C152.1 | 3 | 3 | 2 | 2 | 2 | 3 | 2 | 2 | 3 |
| C152.2 | 2 | 3 | 3 | 2 | 3 | 2 | 3 | 3 | 2 |
| C152.3 | 2 | 3 | 2 | 2 | 3 | 3 | 3 | 2 | 3 |
| C152.4 | 2 | 3 | 2 | 3 | 2 | 2 | 2 | 2 | 2 |
| C152.5 | 3 | 3 | 2 | 3 | 2 | 2 | 3 | 3 | 3 |

Syllabus of MMT-251 (Practical)

| | | |
|----------------------------|-----------------------|--|
| School: SBSR | | Batch : 2018-20 |
| Program: M.Sc. | | Current Academic Year: 2019-20 |
| Branch: Mathematics | | Semester: III |
| 1 | Course Code | MMT-251 |
| 2 | Course Title | Mathematics Lab III |
| 3 | Credits | 2 |
| 4 | Contact Hours (L-T-P) | 0-0-3 |
| | Course Status | Compulsory |
| 5 | Course Objective | <ul style="list-style-type: none"> To create understanding of the LaTeX and enable the students how to write resume, write question paper, write articles/ research papers. |
| 6 | Course Outcomes | CO1: Understand the procedures installation of the software LaTeX. (K2) CO2: Discuss and explain Latex basic syntax and write equations, matrix, and tables. (K2, K4, K6) CO3: Explain and write page layout, equation references citation tables of contents list of figures etc. (K2, K4, K6) CO4: Describe how to write Geometry, Hyperref, amsmath, amssymb, algorithms in Latex. (K1, K2, K6) CO5: Discuss the classes and explain how to write article, book, report, beamer, slides. IEEtran. . (K2,K4, K6) CO6: Write resume, question paper, research paper, project in Latex . (K2, K5, K6) |
| 7 | Course Description | This course teaches the LaTeXTo and describes how to write resume, write question paper, and write articles / research papers. |
| 8 | Outline syllabus | CO Mapping |
| | Unit 1 | Lab. Experiment 1: |
| | | Installation of the software LaTeX |
| | | Understanding Latex compilation: Basic Syntex, Writing equations, Matrix, Tables |
| | Unit 2 | Lab. Experiment 2: |
| | | Page Layout – Titles, Abstract Chapters, Sections, References, Equation references, citation. List making environments Table of contents, Generating new commands, Figure handling numbering, List of figures, List of tables, Generating index. |
| | Unit 3 | Lab. Experiment 3: |
| | | Packages: Geometry, Hyperref, amsmath, amssymb, |
| | | CO4 |

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| | | algorithms, algorithmic graphic, color, tilez listing. | |
| | Unit 4 | Lab. Experiment 4: | |
| | | Classes: article, book, report, beamer, slides. IEEtran. | CO5 |
| | Unit 5 | Lab. Experiment 5: | |
| | | Applications to: Writing resume Writing question paper Writing articles/ research papers | CO6 |
| | Mode of examination | Practical | |
| | Weightage Distribution | CA MTE ETE | |
| | | 60% 0% 40% | |
| | Text book/s* | LATEX for Beginners | |
| | Other References | | |

COURSE OUTCOMES – PROGRAMME OUTCOMES MAPPING TABLE

| PO CO | PO1 | PO2 | PO3 | PO4 | PO5 | PSO1 | PSO2 | PSO3 | PSO4 |
|----------|-----|-----|-----|-----|-----|------|------|------|------|
| C251.1 | 3 | 3 | 2 | 2 | 2 | 3 | 2 | 2 | 3 |
| C251.2 | 2 | 3 | 3 | 2 | 3 | 2 | 3 | 2 | 2 |
| C251.3 | 2 | 3 | 2 | 2 | 3 | 3 | 3 | 2 | 2 |
| C251.4 | 2 | 3 | 2 | 2 | 2 | 2 | 2 | 2 | 2 |
| C251.5 | 3 | 3 | 2 | 2 | 2 | 2 | 3 | 3 | 3 |

Syllabus of Project I

| | | | | | |
|---------------------|------------------------|--|-----|-----|----------------|
| School: SBSR | | Batch : 2018-20 | | | |
| Program: M.Sc. | | Current Academic Year: 2019-20 | | | |
| Branch: Mathematics | | Semester: III | | | |
| 1 | Course Code | MMT 252 | | | |
| 2 | Course Title | DISSERTATION-I | | | |
| 3 | Credits | 2 | | | |
| 4 | Contact Hours (L-T-P) | 0-0-3 | | | |
| | Course Status | Compulsory/Elective | | | |
| 5 | Course Objective | <ul style="list-style-type: none">• Deep knowledge of a specific area of specialization.• Develop communication skills especially in project writing and oral presentation. Develop some time management skills. | | | |
| 6 | Course Outcomes | CO1: Explain the concept of research within the subject, as regards approaching a question, collecting and analysing background material and presenting research questions and conclusions. (K2, K4) CO2: Construct and develop a deeper interest in mathematics and taste for research. (K5, K6) CO3: Select and recommend the activities that support their professional goals. (K4, K6) CO4: Develop effective project organizational skills. (K5) | | | |
| 7 | Course Description | Maintain a core of mathematical and technical knowledge that is adaptable to changing technologies and provides a solid foundation for future learning. | | | |
| 8 | Outline syllabus | | | | CO Achievement |
| | Unit 1 | Introduction | | | CO1 |
| | | | | | |
| | Unit 2 | Case study | | | CO1,CO2 |
| | | | | | |
| | Unit 3 | Conceptual | | | CO2,CO3 |
| | | | | | |
| | Unit 4 | Development | | | CO3 |
| | | | | | |
| | Unit 5 | Finalisation | | | CO3,CO4 |
| | | | | | |
| | Mode of examination | Jury/Practical/Viva | | | |
| | Weightage Distribution | CA | MTE | ETE | |
| | | 60% | 0% | 40% | |
| | Text book/s* | - | | | |
| | Other References | | | | |

COURSE OUTCOMES – PROGRAMME OUTCOMES MAPPING TABLE

| PO | PO1 | PO2 | PO3 | PO4 | PO5 | PSO1 | PSO2 | PSO3 | PSO4 |
|--------|-----|-----|-----|-----|-----|------|------|------|------|
| CO | | | | | | | | | |
| C252.1 | 3 | 3 | 2 | 2 | 2 | 3 | 2 | 3 | 3 |
| C252.2 | 2 | 3 | 3 | 2 | 3 | 2 | 3 | 3 | 2 |
| C252.3 | 2 | 3 | 2 | 2 | 3 | 3 | 3 | 3 | 3 |
| C252.4 | 2 | 3 | 2 | 2 | 2 | 3 | 2 | 3 | 2 |

Syllabus of Project II

| | | | |
|----------------------------|-----------------------|--|--|
| School: SBSR | | Batch : 2018-20 | |
| Program: B.Sc. | | Current Academic Year: 2019-20 | |
| Branch: Mathematics | | Semester: IV | |
| 1 | Course Code | MMT 253 | |
| 2 | Course Title | DISSERTATION-2 | |
| 3 | Credits | 8 | |
| 4 | Contact Hours (L-T-P) | 0-0-8 | |
| | Course Status | Compulsory/Elective | |
| 5 | Course Objective | <ul style="list-style-type: none"> Deep knowledge of a specific area of specialization. Develop communication skills especially in project writing and oral presentation. Develop some time management skills. | |
| 6 | Course Outcomes | CO1: Explain the concept of research within the subject, as regards approaching a question, collecting and analysing background material and presenting research questions and conclusions. (K2, K4) CO2: Construct and develop a deeper interest in mathematics and taste for research. (K5, K6) CO3: Select and recommend the activities that support their professional goals. (K4, K6) CO4: Develop effective project organizational skills. (K5) | |
| 7 | Course Description | Maintain a core of mathematical and technical knowledge that is adaptable to changing technologies and provides a solid foundation for future learning. | |

| | | | | |
|---|------------------------|---------------------|-----------|----------------|
| 8 | Outline syllabus | | | CO Achievement |
| | Unit 1 | Introduction | | CO1 |
| | Unit 2 | Case study | | CO1,CO2 |
| | Unit 3 | Conceptual | | CO2,CO3 |
| | Unit 4 | Development | | CO3 |
| | Unit 5 | Finalisation | | CO3,CO4 |
| | Mode of examination | Jury/Practical/Viva | | |
| | Weightage Distribution | CA 60% | MTE 0% | ETE 40% |
| | Text book/s* | - | | |
| | Other References | | | |

COURSE OUTCOMES – PROGRAMME OUTCOMES MAPPING TABLE

| PO CO | PO1 | PO2 | PO3 | PO4 | PO5 | PSO1 | PSO2 | PSO3 | PSO4 |
|----------|-----|-----|-----|-----|-----|------|------|------|------|
| C253.1 | 3 | 3 | 2 | 2 | 2 | 3 | 2 | 3 | 3 |
| C253.2 | 2 | 3 | 3 | 2 | 3 | 2 | 3 | 3 | 2 |
| C253.3 | 2 | 3 | 2 | 2 | 3 | 3 | 3 | 3 | 3 |
| C253.4 | 2 | 3 | 2 | 2 | 2 | 3 | 2 | 3 | 2 |

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